

The last electromagnetic breath of binary black holes

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Tenure-track researcher

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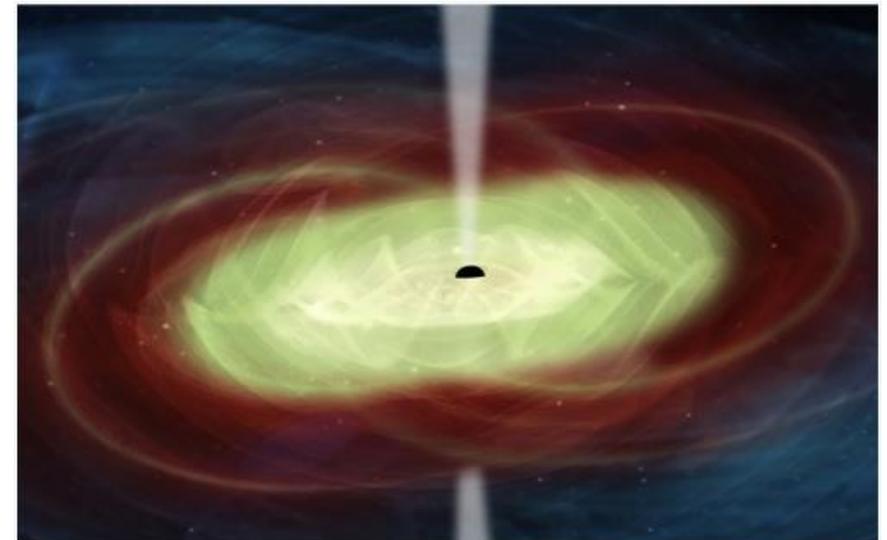
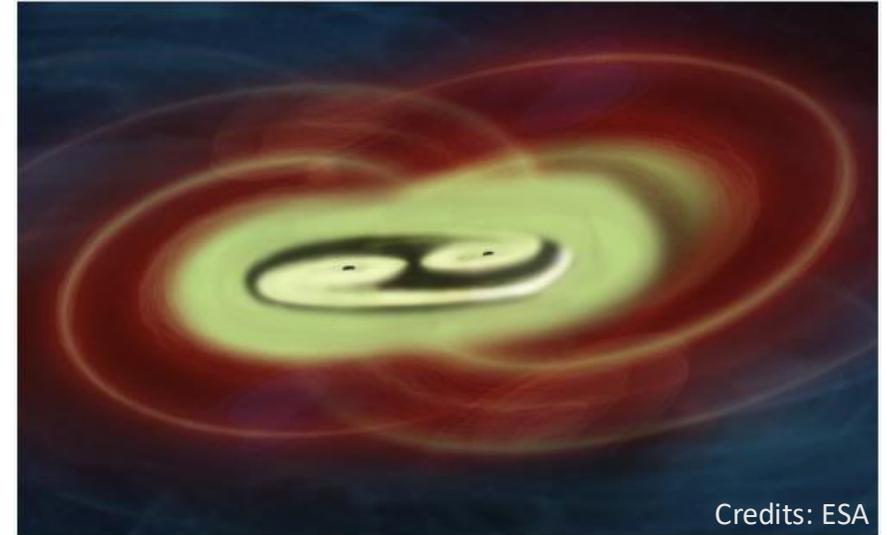
Electromagnetic counterpart to binary black hole merger



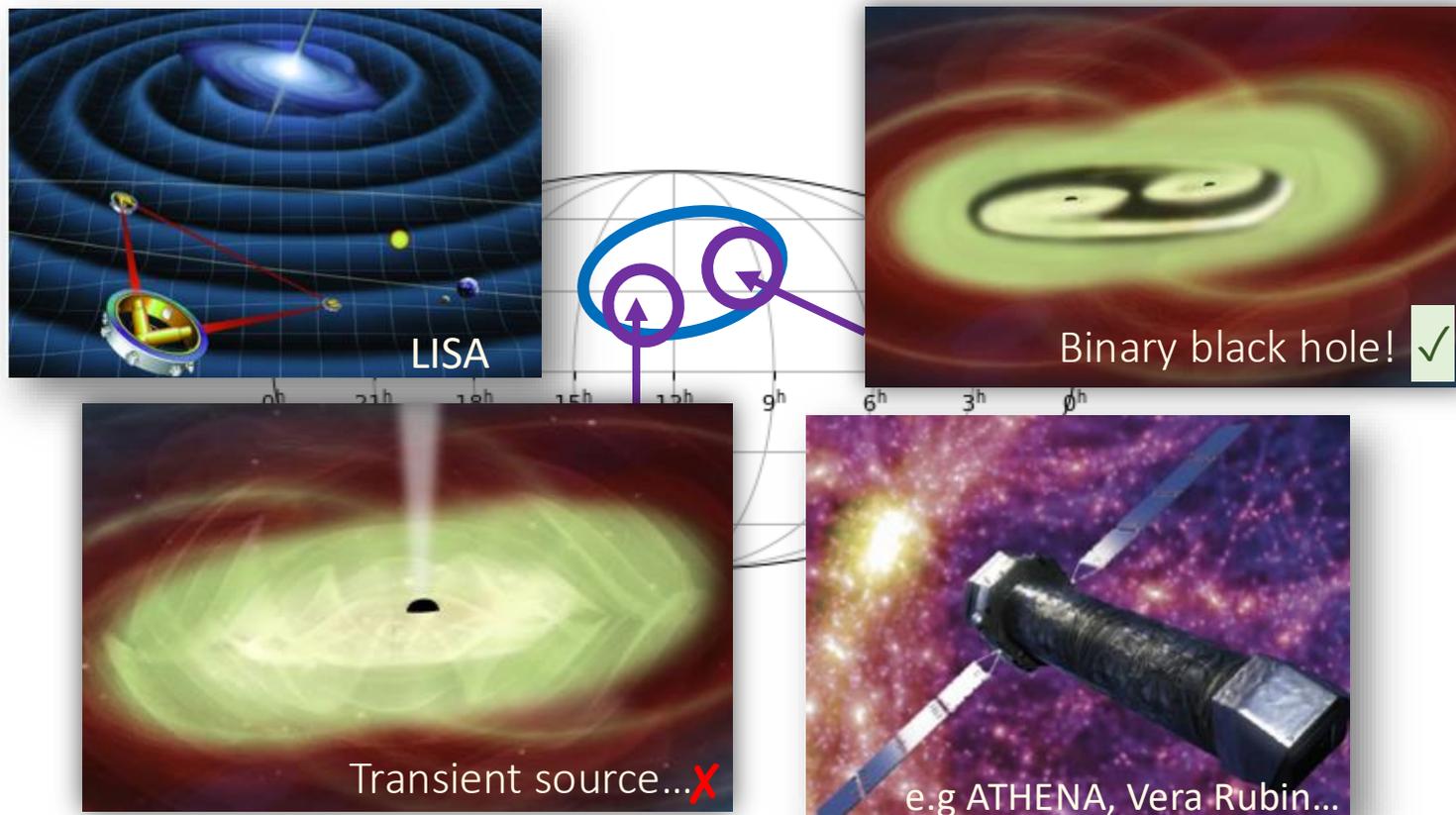
Need a gas-rich environment:
e.g. galaxy merger
or AGN disk (Graham+20,+22)

○ Binary black holes and their coalescence

- Galaxy + black hole growth
- Cosmology: Hubble constant
- Fundamental physics: speed of gravity
- Formation of active galactic nuclei?



Identification of BBHs before/after GW detection



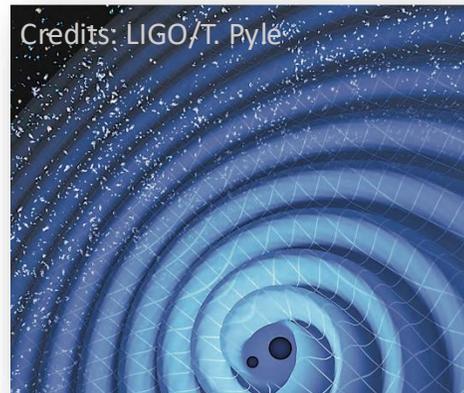
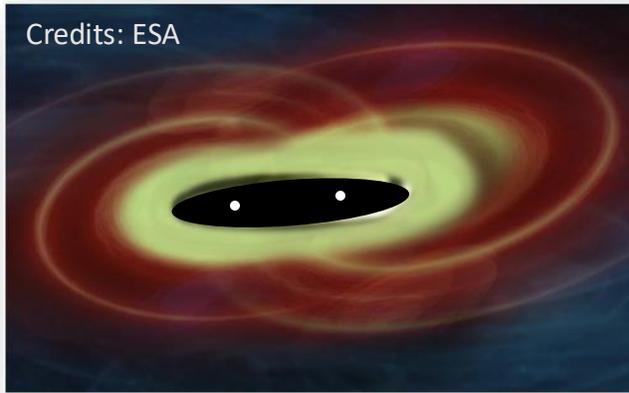
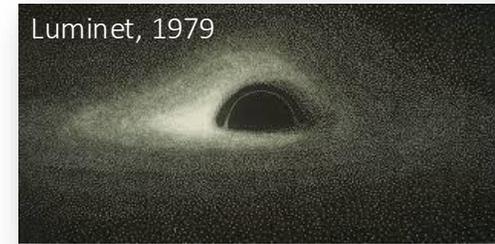
- LISA: space-based gravitational wave detector
0.1-100 mHz band
 - BBHs $10^{4-7}M_{\odot}$: ~ 10 days before merger

- PTA: Pulsar Timing Arrays
1nHz-100nHz band
 - Close individual BBHs $10^{7-10}M_{\odot}$ mergers

How to distinguish binary black holes from other (transient) sources ?

Modelling a BBH and its circumbinary disk

- **GR-AMRVAC** code (Keppens+12, GR: Casse+17)
- How does the fluid know about the binary black hole?
 - Newtonian gravity? (e.g. D’Orazio+13)
 - Solving the Einstein’s equations? (e.g. Einstein Toolkit, Löffler+12)



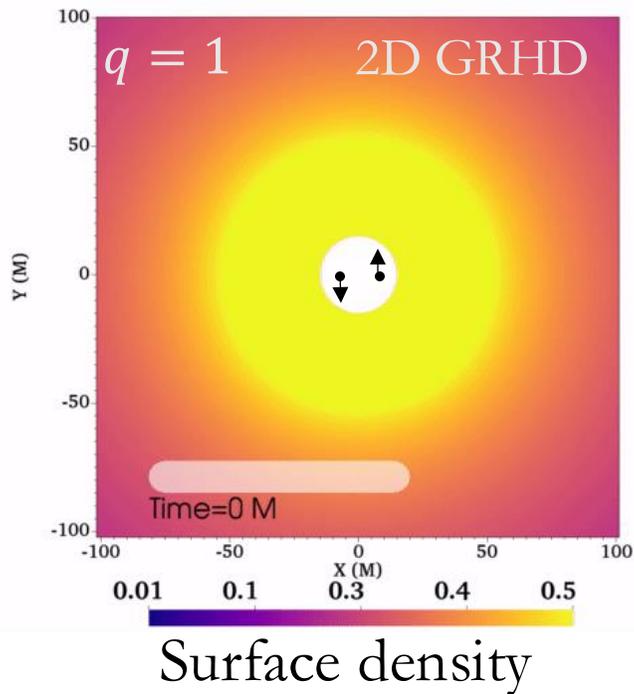
- Extend GR-AMRVAC to dynamical spacetimes + implement approximate analytical BBH metric valid in the circumbinary region (Mignon-Risse et al. 2022, MNRAS)

- Still, a computationally-heavy, and conceptually more complex, construction (see e.g. Ireland+16):

$$g_{00} + 1 = \frac{2m_1}{r} + \frac{m_1}{r} \left\{ v_1^2 - \frac{m_2}{b} + 2(\vec{v}_1 \cdot \hat{n})^2 - \frac{2m}{r} + 6 \frac{(\vec{x}_1 \cdot \hat{n})}{r} (\vec{v}_1 \cdot \hat{n}) - \frac{x_1^2}{r^2} + \frac{(\vec{x}_1 \cdot \hat{n})^2}{r^2} (3 - 2r^2\omega^2) \right\} + (1 \leftrightarrow 2) + O(v^5),$$

- Construction valid until the BBH motion becomes relativistic

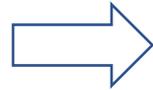
Circular orbits: accretion structures and EM variability



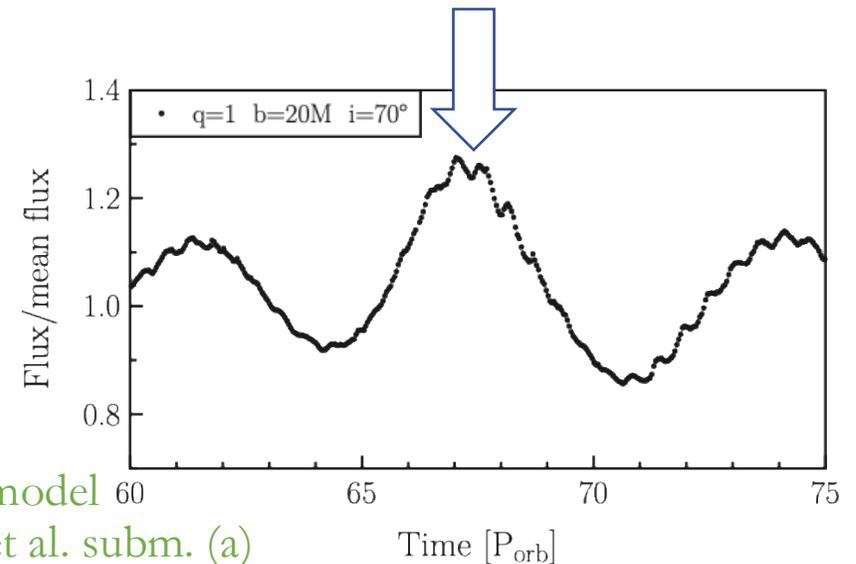
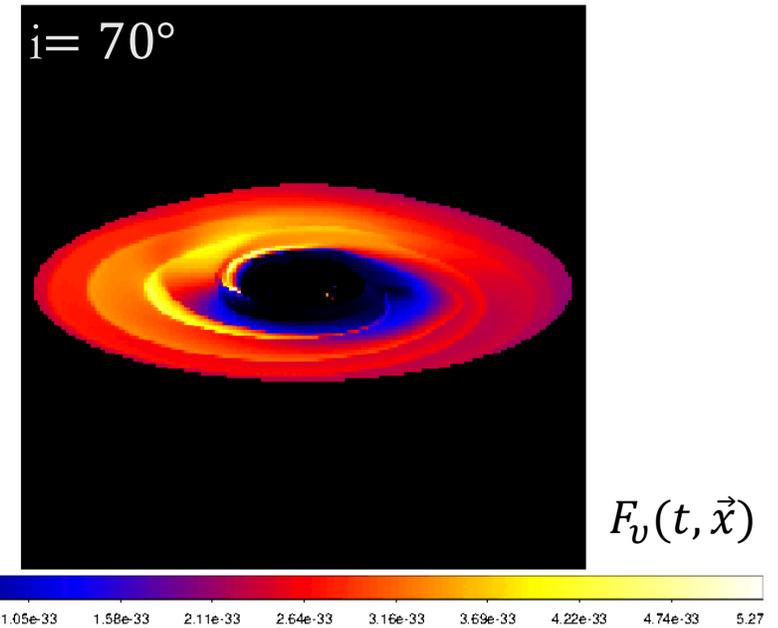
1. Cavity at $\sim 2x$ separation (Artymowicz+94)
2. **Streams** (Artymowicz+96) & **spiral arms**
3. **An overdensity, or « lump »**
(e.g. MacFadyen+08, Shi+12, Noble+12, Mignon-Risse+23...)



- GR ray-tracing in BBH metric with GYOTO (Vincent+11)
no fast-light approximation



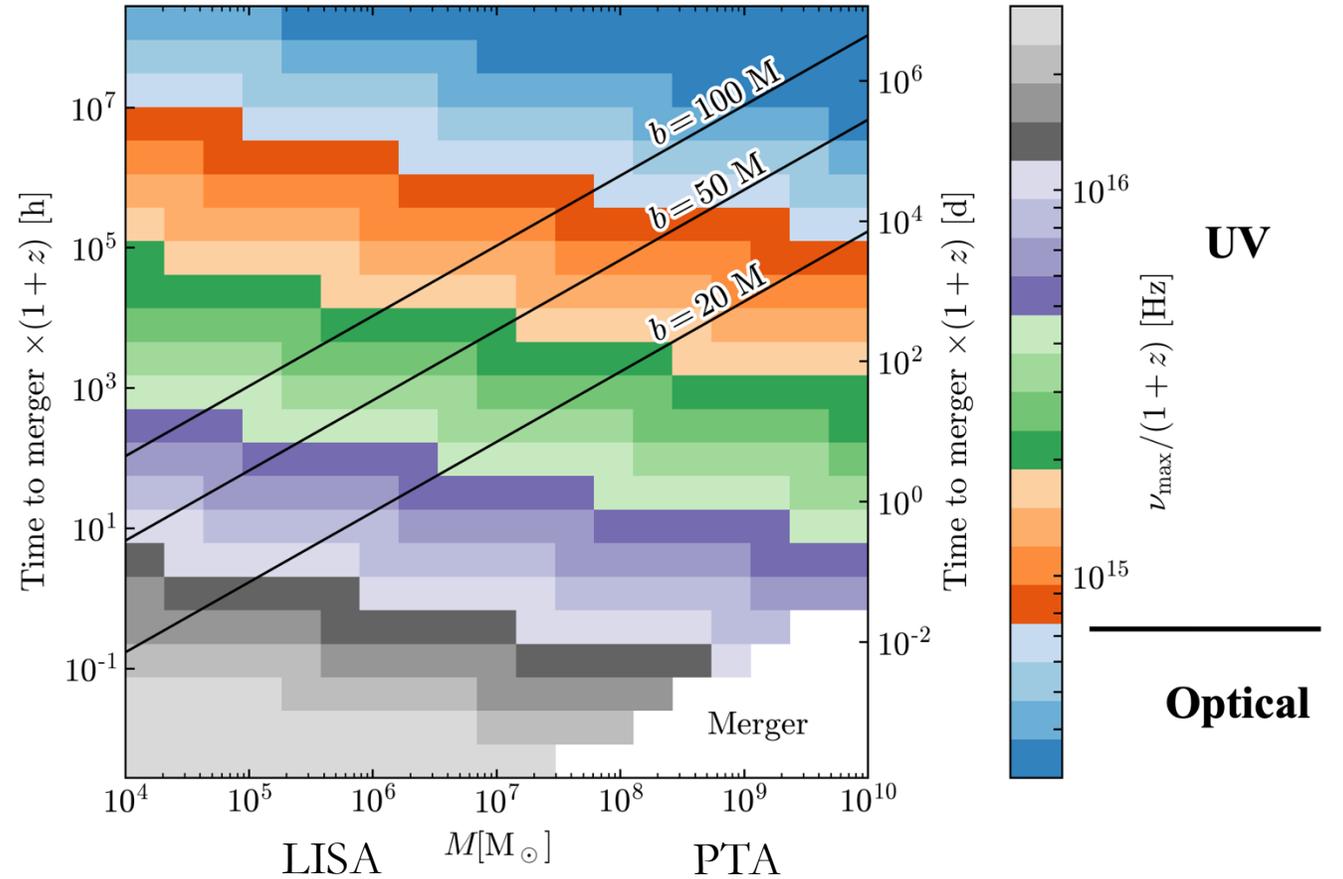
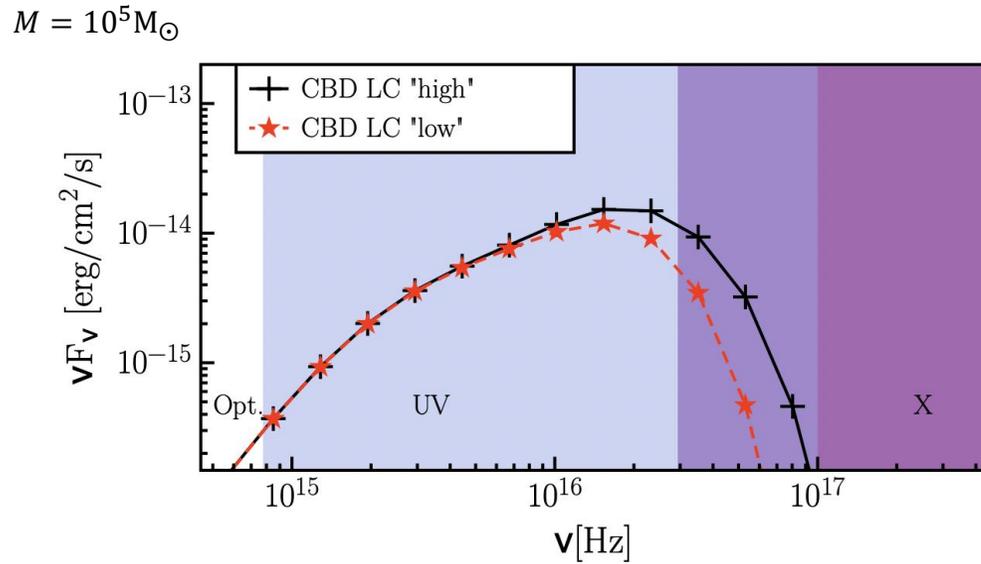
- Simple thermodynamical model
 $T \sim \Sigma^{\gamma-1}, \gamma = 5/3$



Which frequency band to observe this modulation?

For $q = 1, \dot{M} = 0.5 \dot{M}_{\text{Edd}}$

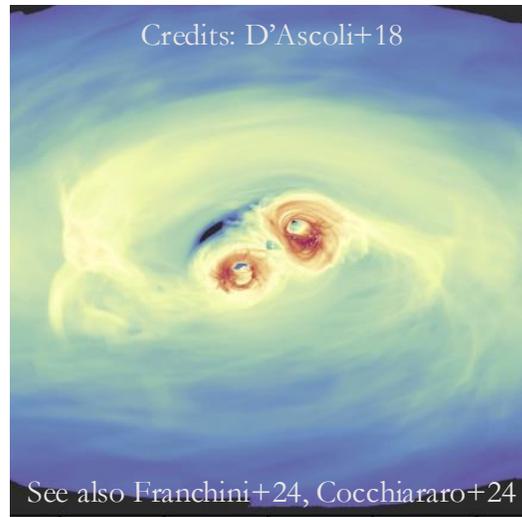
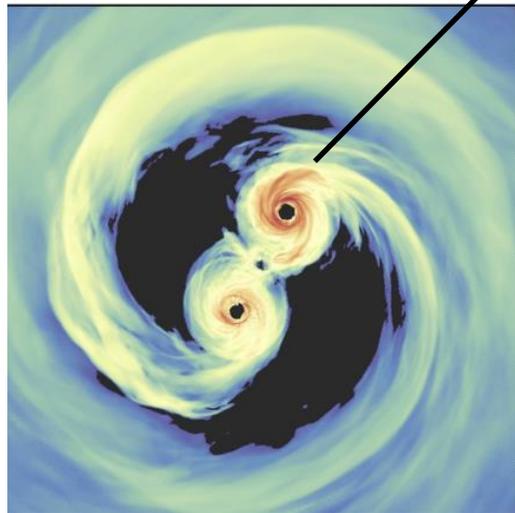
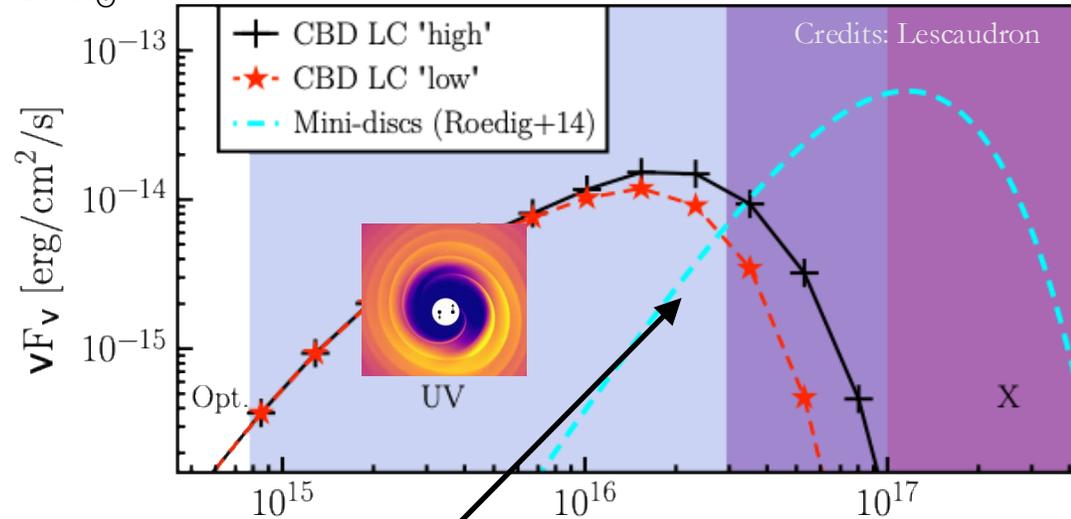
Time-to-merger estimated analytically (Peters 1964)



→ UV/optical for most LISA/PTA sources

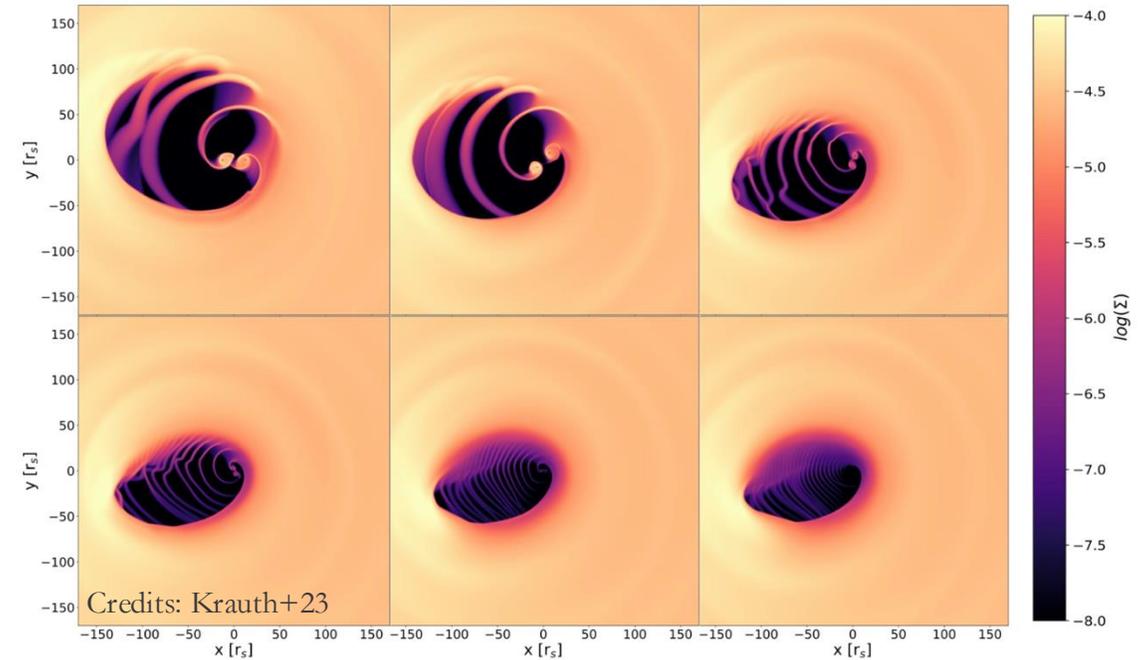
Higher-frequency EM signatures from individual disks but...

$M = 10^5 M_\odot$



but...

- Gas plunges → weak radiative efficiency (Gutiérrez+22)
- Between (inner) last stable orbit and (outer) tidal truncation → mini-disk disappearance (no GR: Krauth+23+25, Franchini+24)



- Only the circumbinary disk remains
- but BBH inspirals faster: binary-disk « decoupling »
e.g. Armitage & Natarayan 2002

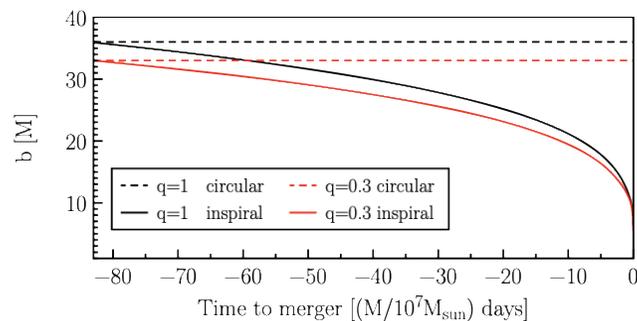
- Expected X-ray emission from « mini-disks »

→ Survival of EM lump modulation « post-decoupling »?

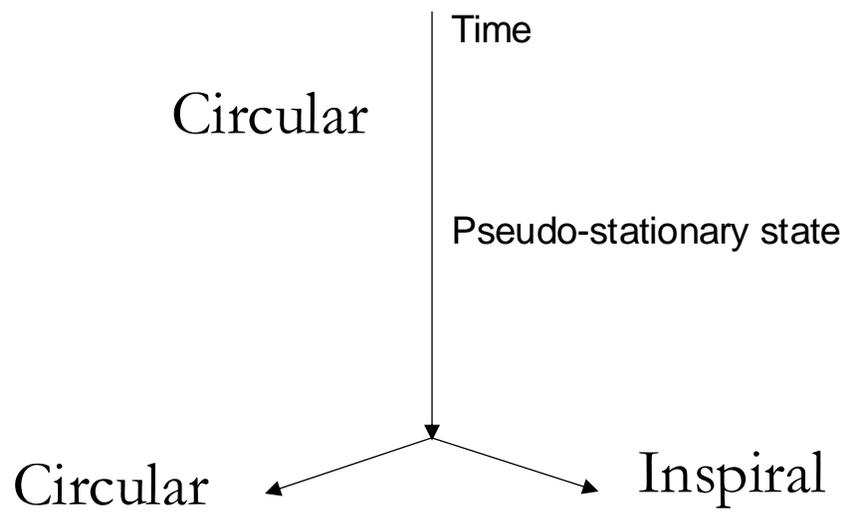
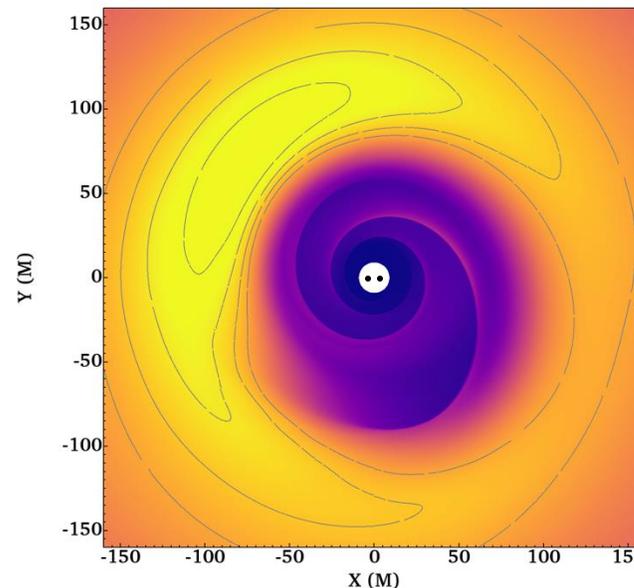
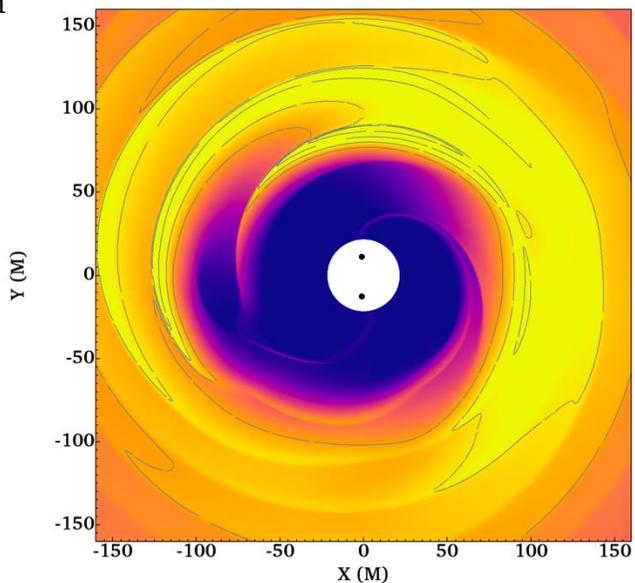
Modelling the inspiral

$$q \in [0.3, 1]$$

$$\text{Time to merger : } 80 \frac{M}{10^7 M_{\odot}} \text{ days}$$



3.5 PN equation of motion

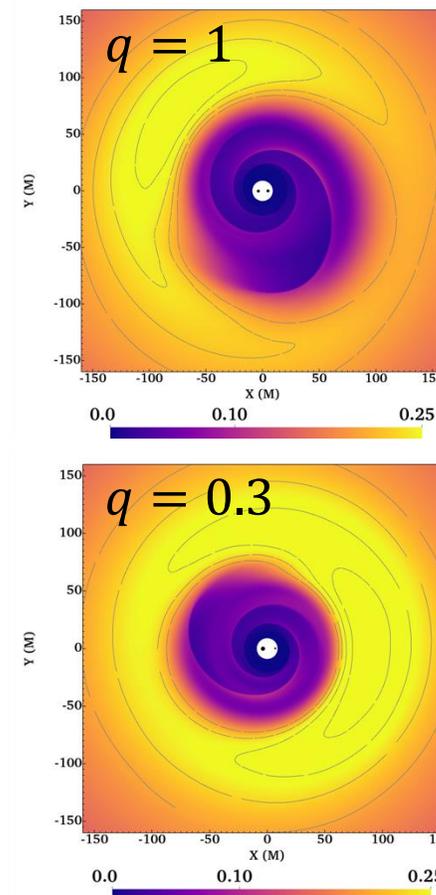
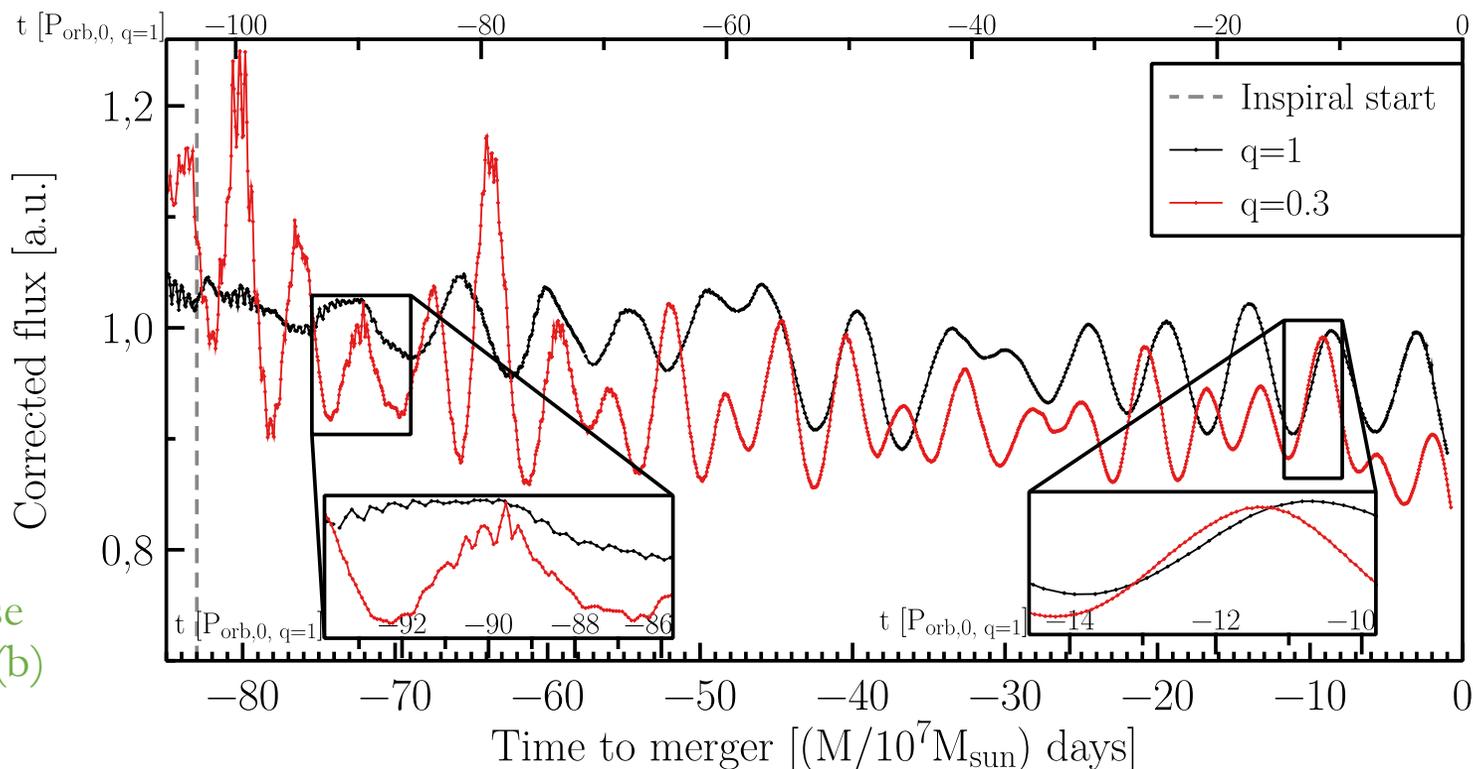


- Numerical challenges :
- Moving inner boundary
 - Spatial resolution disk edge
 - Inspiral time $\propto r_{12}^4$
 - Inspiral time $\propto (1 + q)^2 / 4q$

Electromagnetic signatures post-decoupling

$80 \frac{M}{10^7 M_{\odot}}$ days
before merger

$< 1 \frac{M}{10^7 M_{\odot}}$ day
before merger

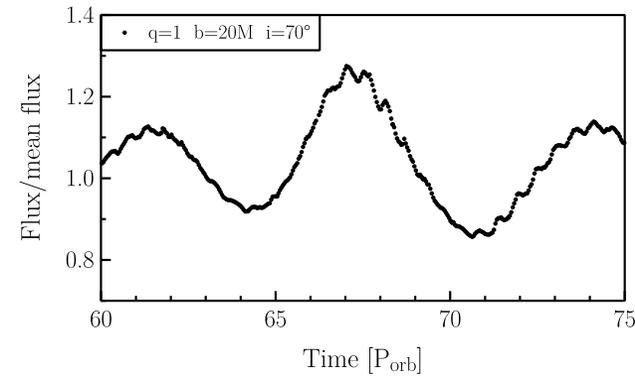
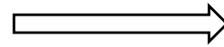
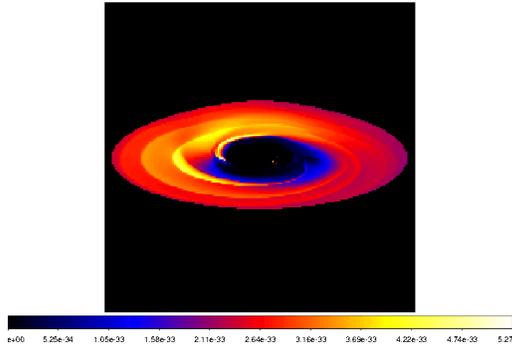


Mignon-Risse
et al. subm. (b)

The lump and its modulation survive post-decoupling

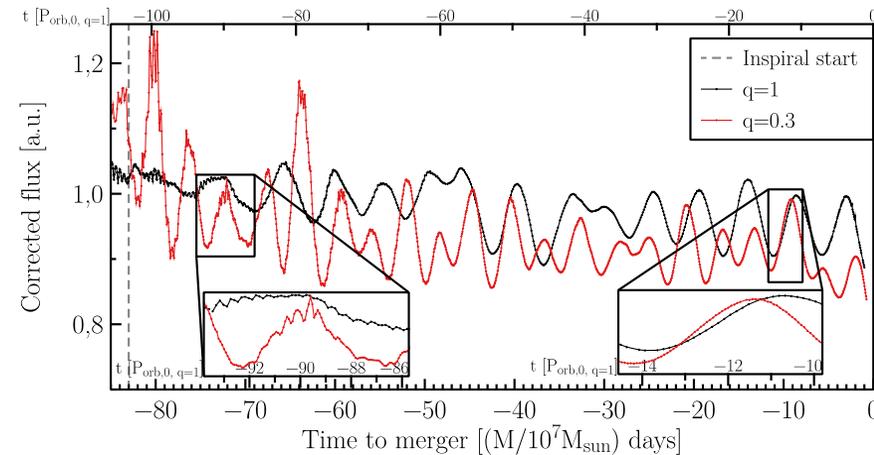
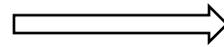
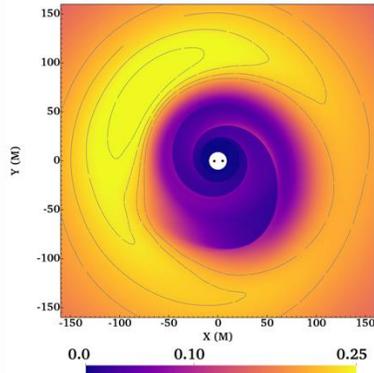
Conclusions: EM appearance of pre-merger BBHs

➤ EM variability in the circular-orbit case



$q \in \{0.1, 0.3, 1\}$
MR+subm. (a)

➤ Lump modulation survival post-decoupling and until $< 1 \frac{M}{10^7 M_\odot}$ day before merger



MR+subm. (b)

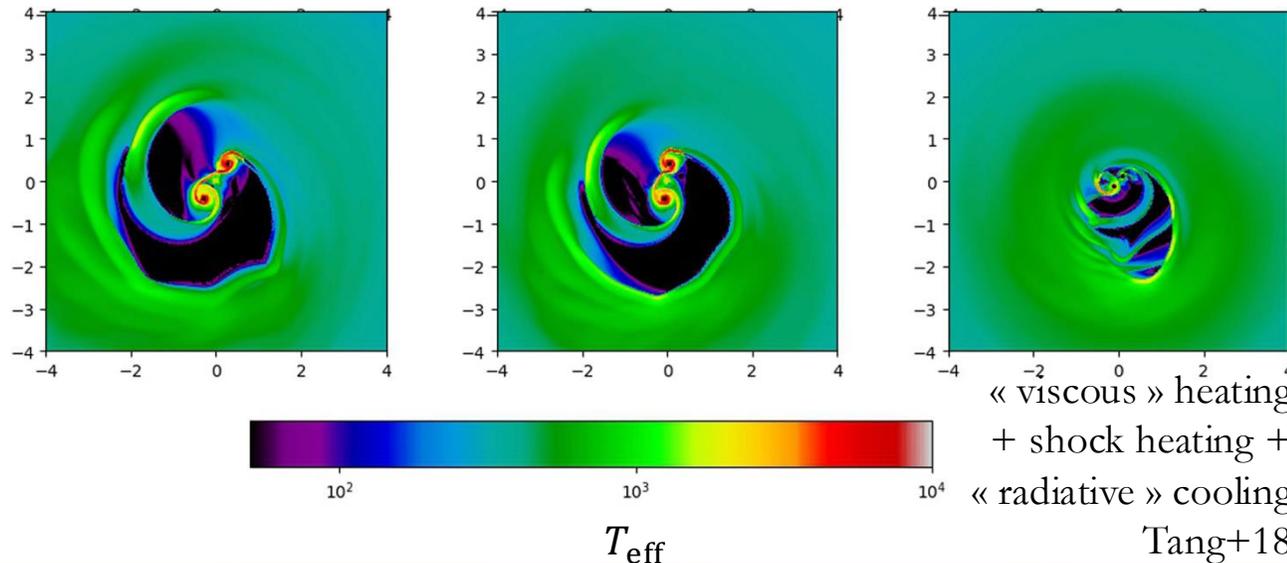
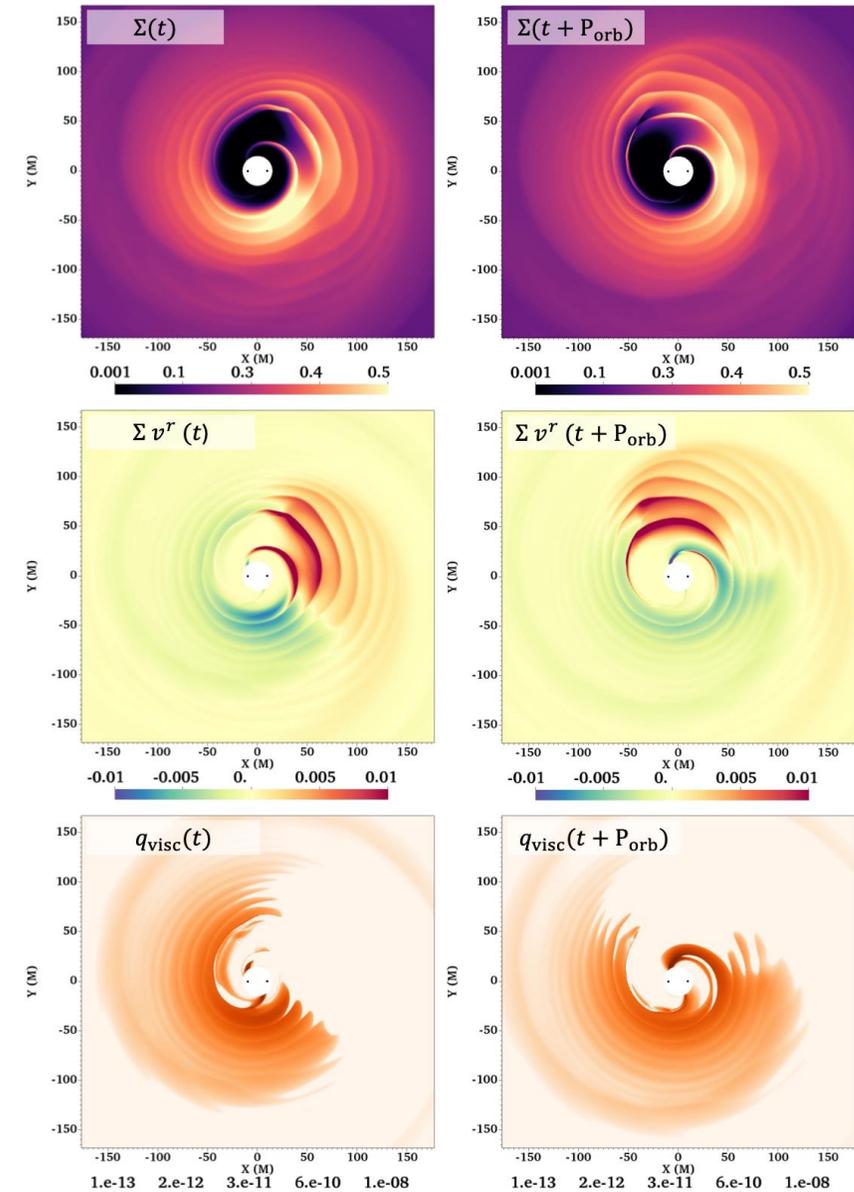
while mini-disks will have disappeared already
The last electromagnetic breath of binary black holes

Viscous-like heating follows the lump's orbit

4.6 Viscous torques

From our discussion of the last section we see that an accretion disc can be an efficient 'machine' for slowly lowering material in the gravitational potential of an accreting object and extracting the energy as radiation. A vital part of this machinery is the process which converts the orbital kinetic energy into heat. The main unsolved problem of disc structure is the precise nature of this: it is surprising (and fortunate) that despite this lack of knowledge considerable progress has been achieved in some areas. Recent progress is beginning to illuminate the nature of viscosity in accretion discs and place some constraints on its magnitude and functional form.

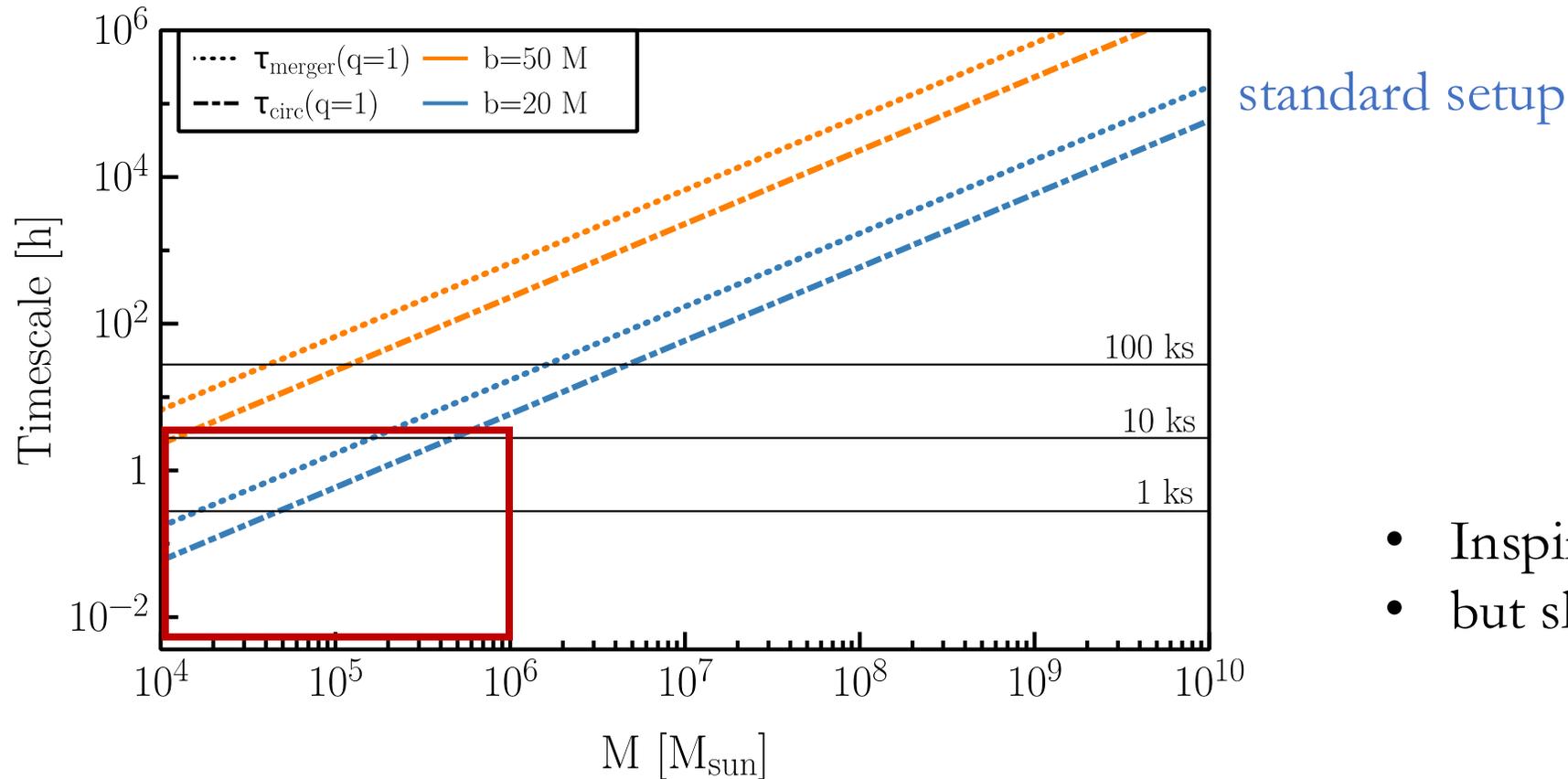
The Accretion Power in Astrophysics
Frank, King & Raine 2003



Impact of inspiral on the EM variability

Q: Is the circular-orbit approximation valid for astrophysical sources ?

- Define τ_{circ} as the time it takes for the separation to decrease by 10% : circular-orbit OK for $\Delta t < \tau_{\text{circ}}$
- Compare τ_{circ} to typical integration times of observations



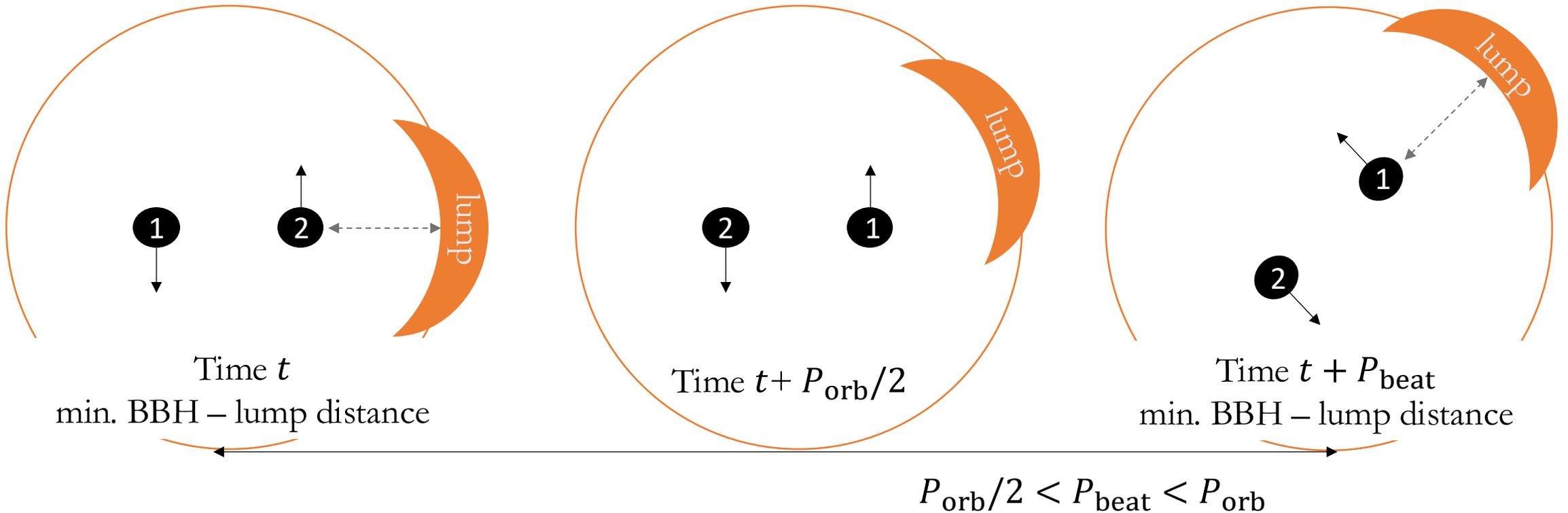
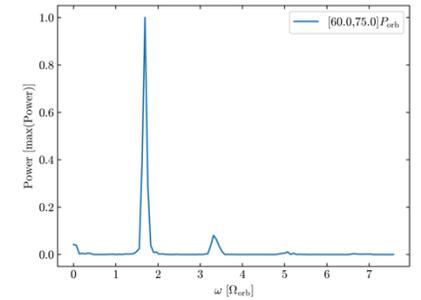
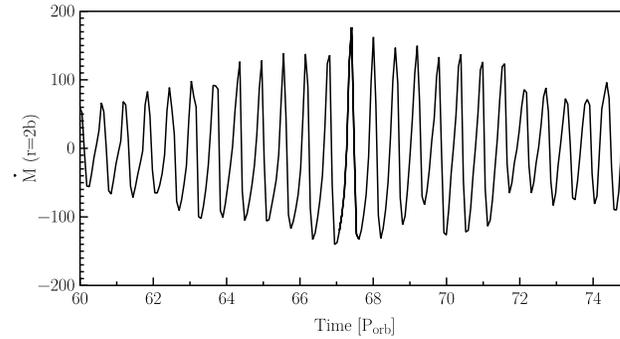
- Inspiral too short for $10^5 M_{\odot}$
- but slowed down if $q < 1$

Need to consider inspiral motion

Fluid simulations: variability

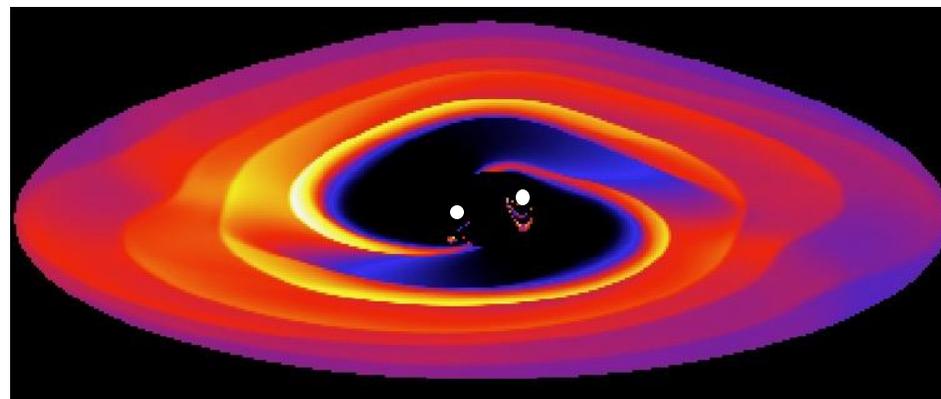
- Accretion rate at $r = 2b \approx$ cavity radius
(same variability at the domain innermost boundary)
 - variability at twice the binary-lump beat frequency

$$2\Omega_{\text{beat}} = 2(\Omega_{\text{orb}} - \Omega_{\text{lump}}) \sim 1.7\Omega_{\text{orb}}$$



Synthetic observations of pre-merger BBHs

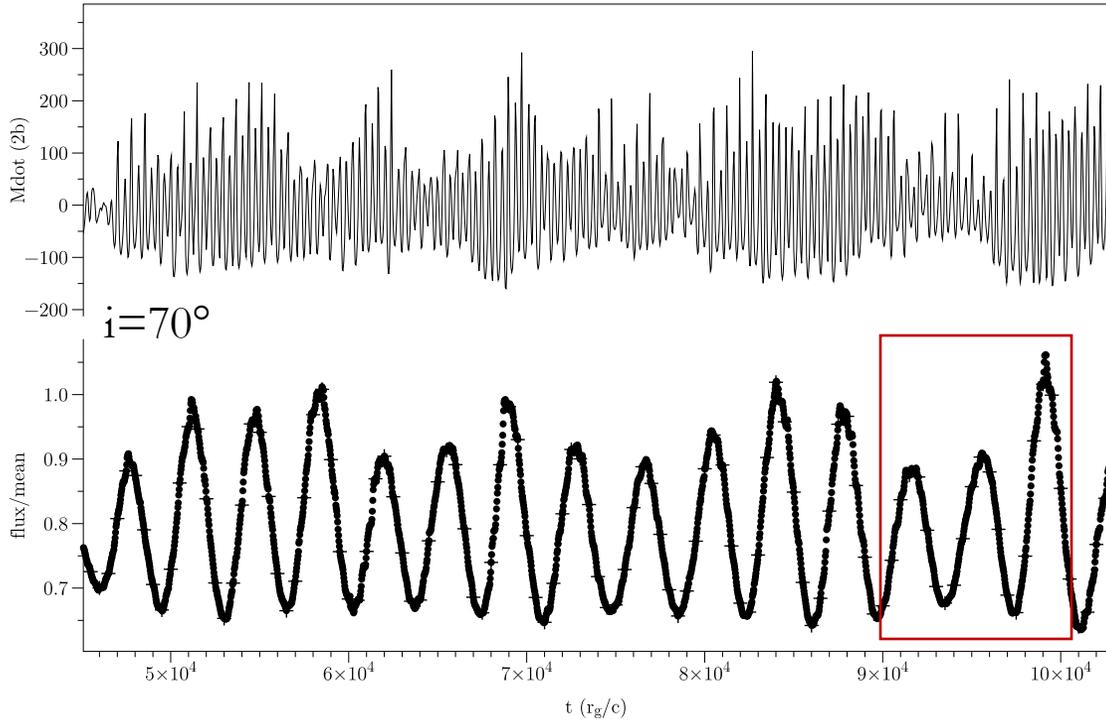
- **GYOTO** code (Vincent+11) incorporating the **BBH approximate metric** (Ireland+16)
 - Thermal emission, thin disk approximation (Shakura & Sunyaev, 1973)
 - Putting physical units back: mass scaling from Lin+13 ($M = 10^5 M_{\odot}$; $T_{\text{in}} = 0.1 \text{ keV}$) as reference
- Obtain the multi-wavelength emission map
- The metric evolves as photons propagate
 - Emission map composed of photons of different time-origin (hence, fluid outputs!)



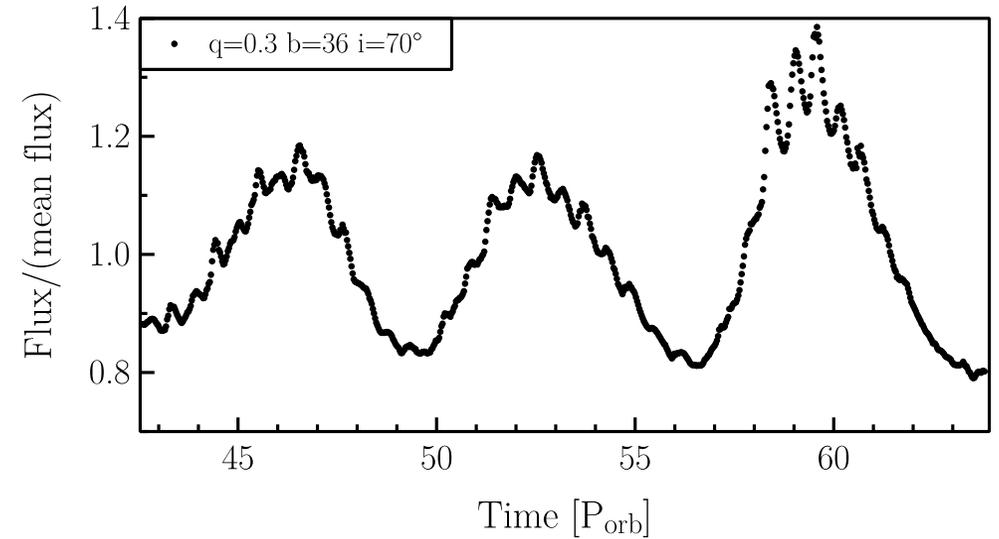
Timing features

- Accretion rate: proxy for the luminosity? (e.g. Krauth+23)

$$q = 0.1; b = 20r_g$$



$$q = 0.3; b = 36r_g$$



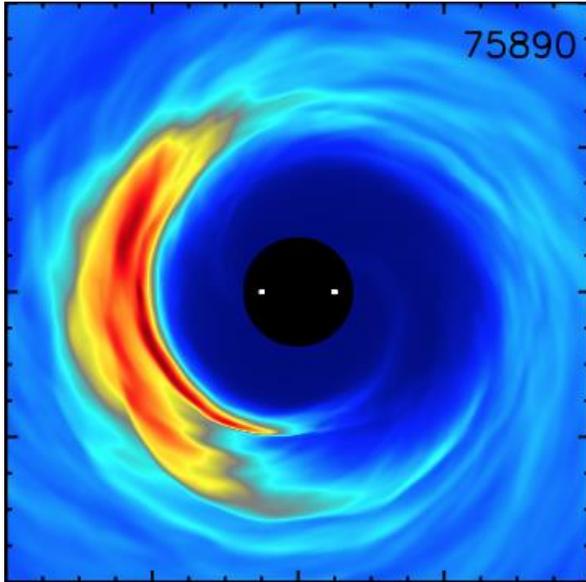
- Additional modulation at the semi-orbital period

$$P_{\text{orb}} = 0.3 \frac{M}{10^6 M_\odot} \text{ ks}$$

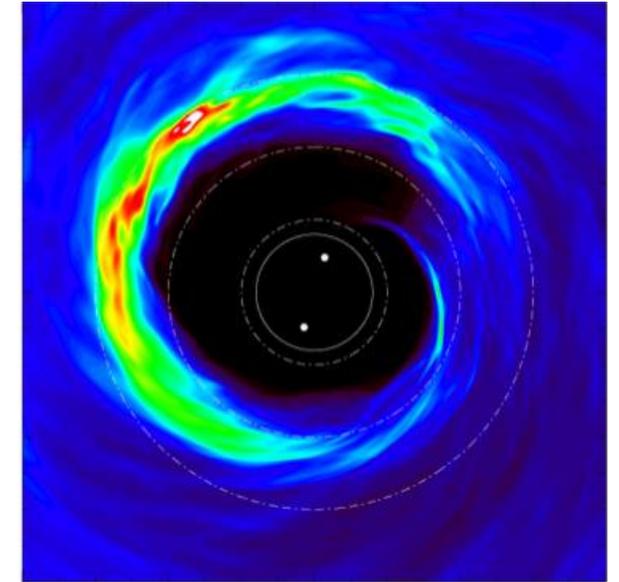
$$P_{\text{lump}} \sim 1.5 \frac{M}{10^6 M_\odot} \text{ ks}$$

Double EM variability: the signature of circumbinary disks around BBHs? (MR+subm.)

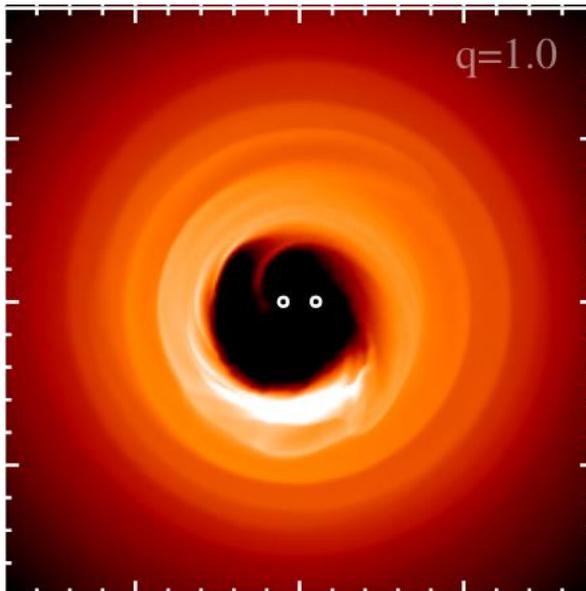
A robust prediction?



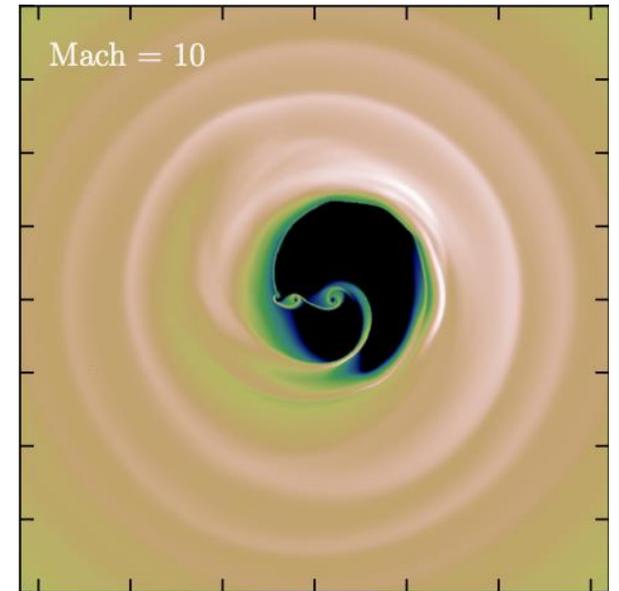
Noble+12, 3D GRMHD



Shi+12, 3D MHD



Ragusa+20, 3D SPH



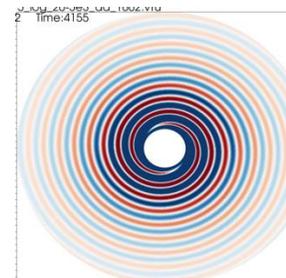
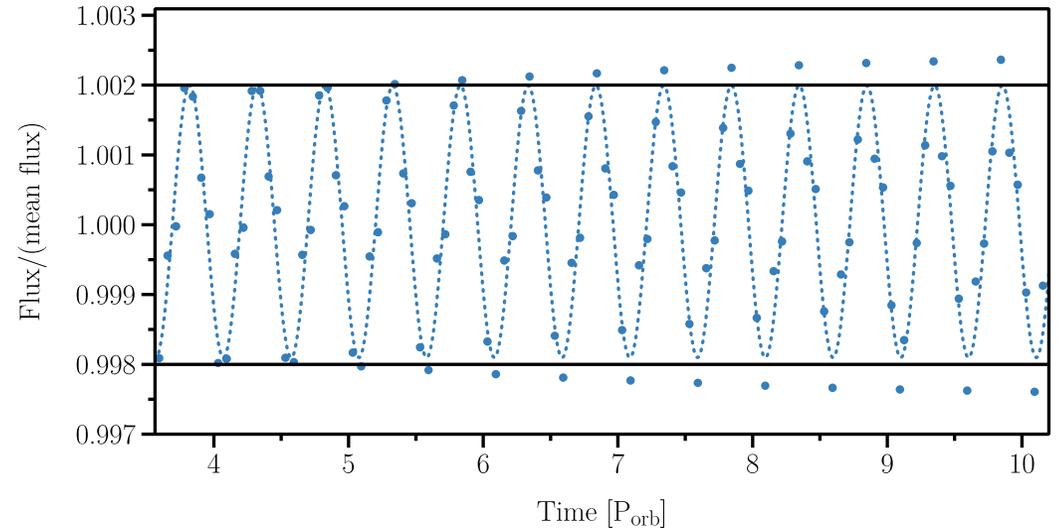
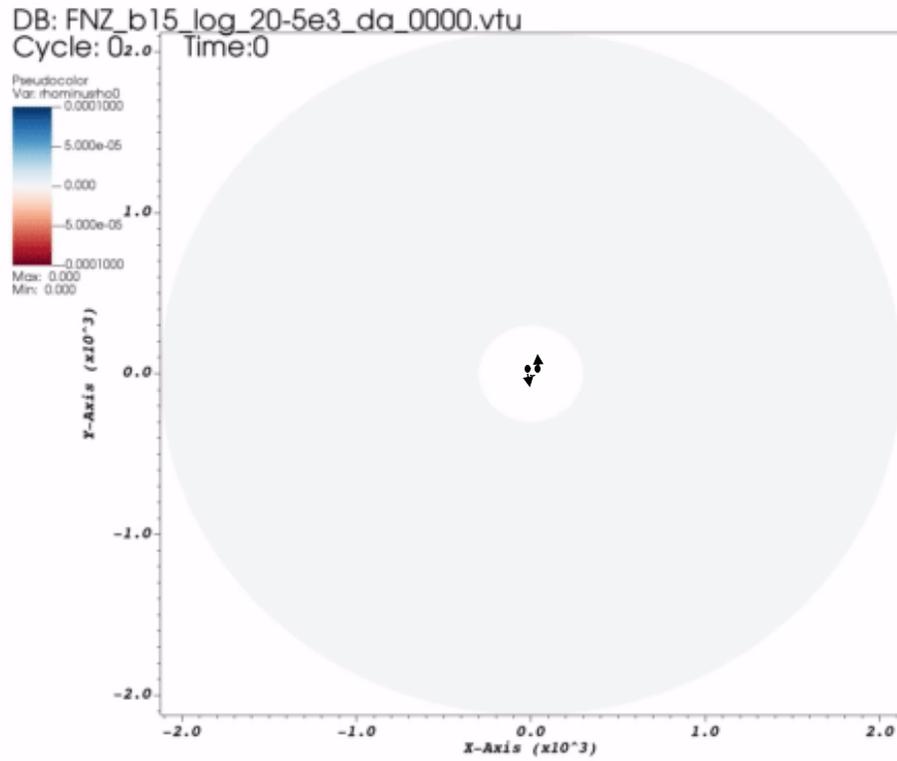
Tiede+20, 2D Hydro

Impact of GWs on the outer disk

Retardation effects?

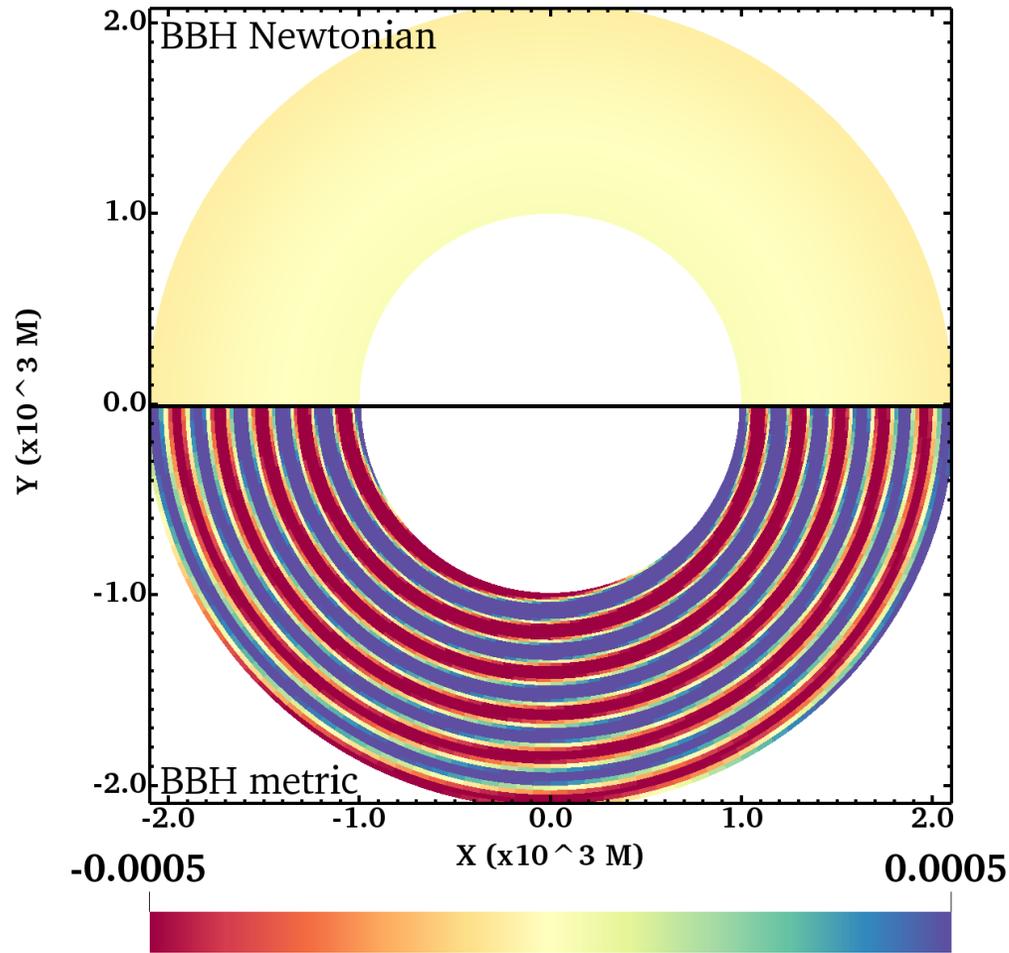
- Disk radius $\sim 2000M = 2000r_g$
- Orbital period $\sim 600M = 600r_g/c$

Weak (<1%) but increasing modulation of the EM flux
Mignon-Risse et al. 2023, *Astronomical Notes*

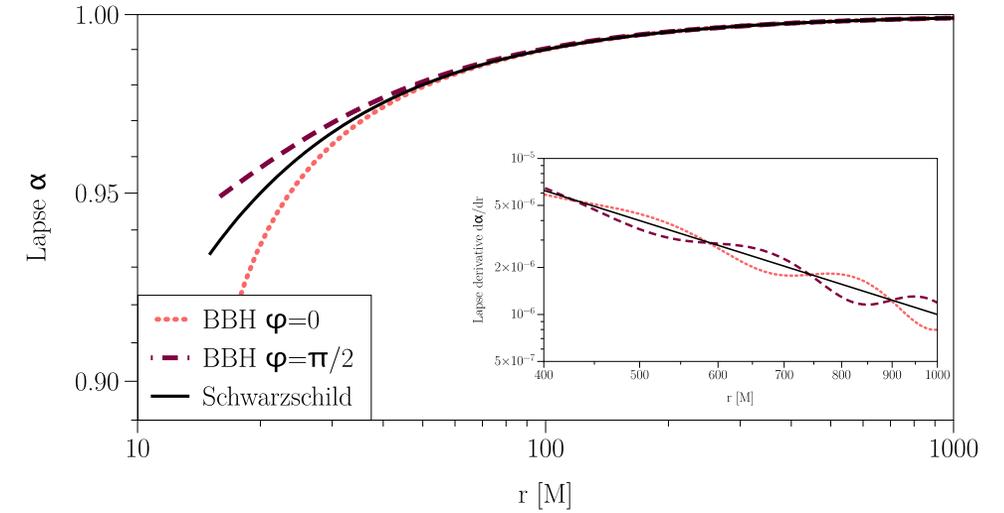


Impact of GWs on the outer disk

1. Not a 2-armed spiral as in Newtonian gravity

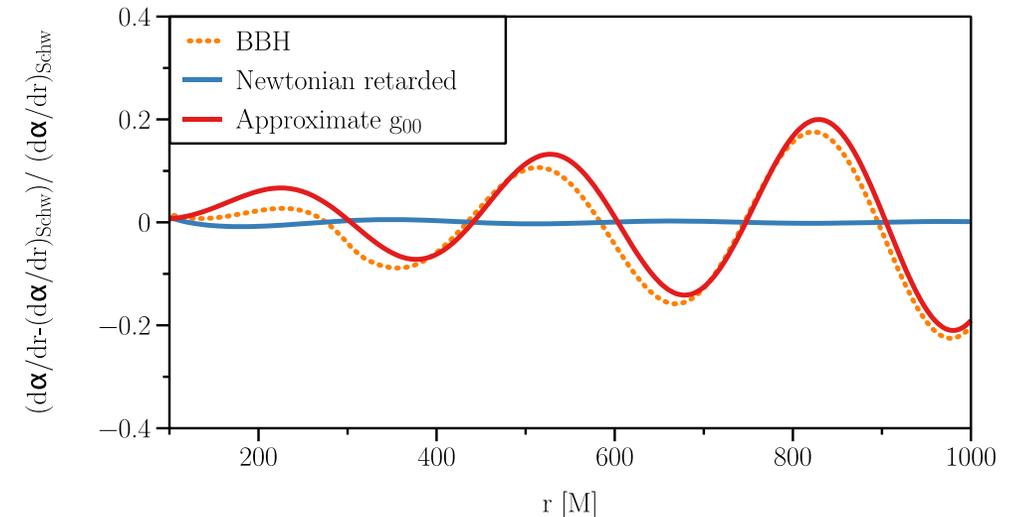


2. Oscillating lapse function: retardation effects \rightarrow GWs



3. Not reproducible with retarded Newtonian potential

4. Diagonal terms of the source stress-energy tensor



A possible instability origin for the lump

i. Why do we care ?

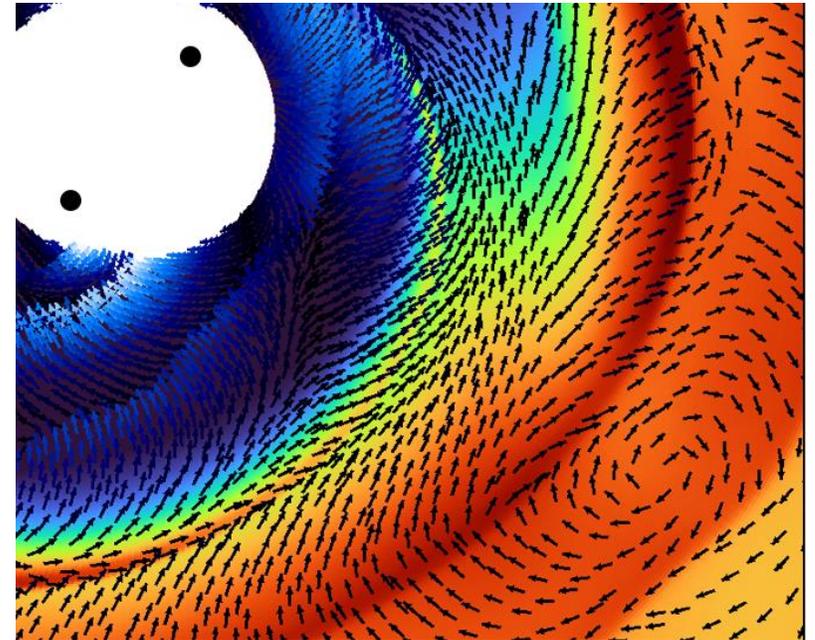
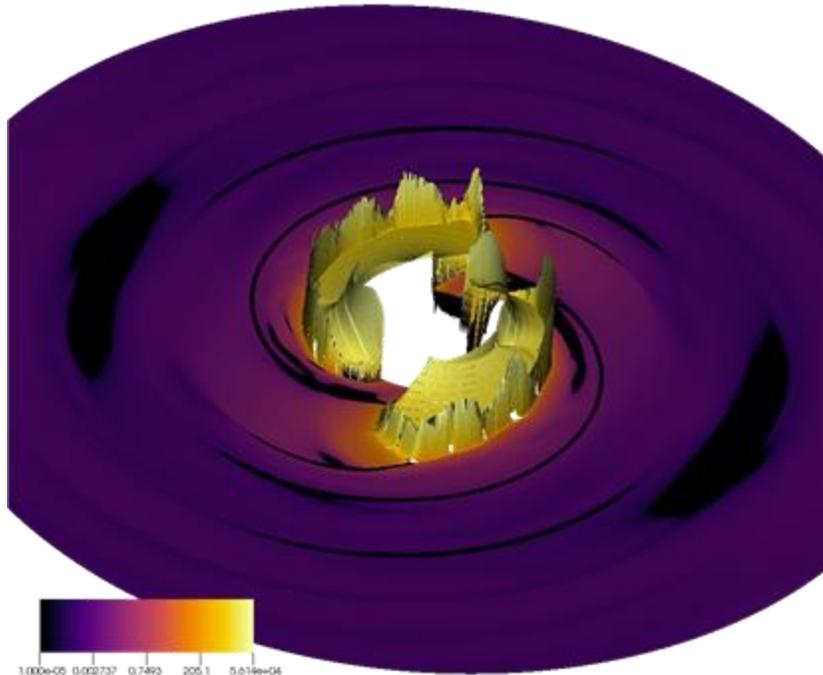
➤ Lump is claimed to be a distinct (observational?) feature of accreting BBHs

ii. Is Rossby Wave Instability a good candidate ?

1. Exponential growth

2. Rossby Wave Instability criterion fulfilled (extremum in vortensity)

3. Presence of vortices

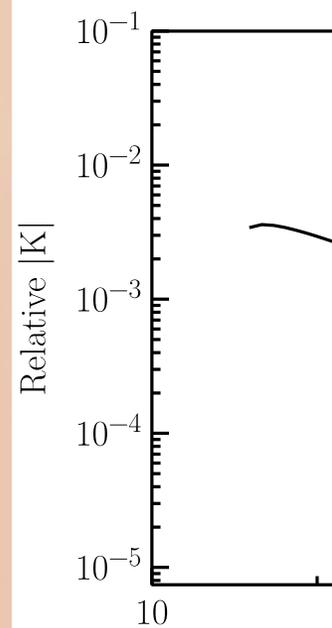


Metric validation

- Correct as displayed

$$\begin{aligned}
 & 605284 \left(\frac{\sqrt{\frac{1}{2}} y \cos\left(\frac{389}{200000} \sqrt{\frac{1}{2}} (t - \sqrt{x^2 + y^2 + z^2})\right)}{\sqrt{x^2 + y^2 + z^2}} - \frac{\sqrt{\frac{1}{2}} x \sin\left(\frac{389}{200000} \sqrt{\frac{1}{2}} (t - \sqrt{x^2 + y^2 + z^2})\right)}{\sqrt{x^2 + y^2 + z^2}} \right)^2 - \frac{2 \left(151321 x^2 + 151321 y^2 + 151321 z^2 - 120000000000 \right) \left(\frac{x \cos\left(\frac{389}{200000} \sqrt{\frac{1}{2}} (t - \sqrt{x^2 + y^2 + z^2})\right)}{\sqrt{x^2 + y^2 + z^2}} + \frac{y \sin\left(\frac{389}{200000} \sqrt{\frac{1}{2}} (t - \sqrt{x^2 + y^2 + z^2})\right)}{\sqrt{x^2 + y^2 + z^2}} \right)}{x^2 + y^2 + z^2} \\
 & + 151321 \cos\left(\frac{389}{200000} \sqrt{\frac{1}{2}} (t - \sqrt{x^2 + y^2 + z^2})\right)^2 + 151321 \sin\left(\frac{389}{200000} \sqrt{\frac{1}{2}} (t - \sqrt{x^2 + y^2 + z^2})\right)^2 \\
 & + \frac{933600000 \left(\frac{\sqrt{\frac{1}{2}} y \cos\left(\frac{389}{200000} \sqrt{\frac{1}{2}} (t - \sqrt{x^2 + y^2 + z^2})\right)}{\sqrt{x^2 + y^2 + z^2}} - \frac{\sqrt{\frac{1}{2}} x \sin\left(\frac{389}{200000} \sqrt{\frac{1}{2}} (t - \sqrt{x^2 + y^2 + z^2})\right)}{\sqrt{x^2 + y^2 + z^2}} \right) \left(\frac{x \cos\left(\frac{389}{200000} \sqrt{\frac{1}{2}} (t - \sqrt{x^2 + y^2 + z^2})\right)}{\sqrt{x^2 + y^2 + z^2}} + \frac{y \sin\left(\frac{389}{200000} \sqrt{\frac{1}{2}} (t - \sqrt{x^2 + y^2 + z^2})\right)}{\sqrt{x^2 + y^2 + z^2}} \right)}{\sqrt{x^2 + y^2 + z^2}} \\
 & - \frac{80000000000 \left(\cos\left(\frac{389}{200000} \sqrt{\frac{1}{2}} (t - \sqrt{x^2 + y^2 + z^2})\right)^2 + \sin\left(\frac{389}{200000} \sqrt{\frac{1}{2}} (t - \sqrt{x^2 + y^2 + z^2})\right)^2 \right)}{x^2 + y^2 + z^2} - \frac{128000000}{\sqrt{x^2 + y^2 + z^2}} - 320000 \\
 g_{tt} = & \frac{16000000 \sqrt{x^2 + y^2 + z^2}}{+ \frac{4}{\sqrt{x^2 + y^2 + z^2}} - 1}
 \end{aligned}$$

view

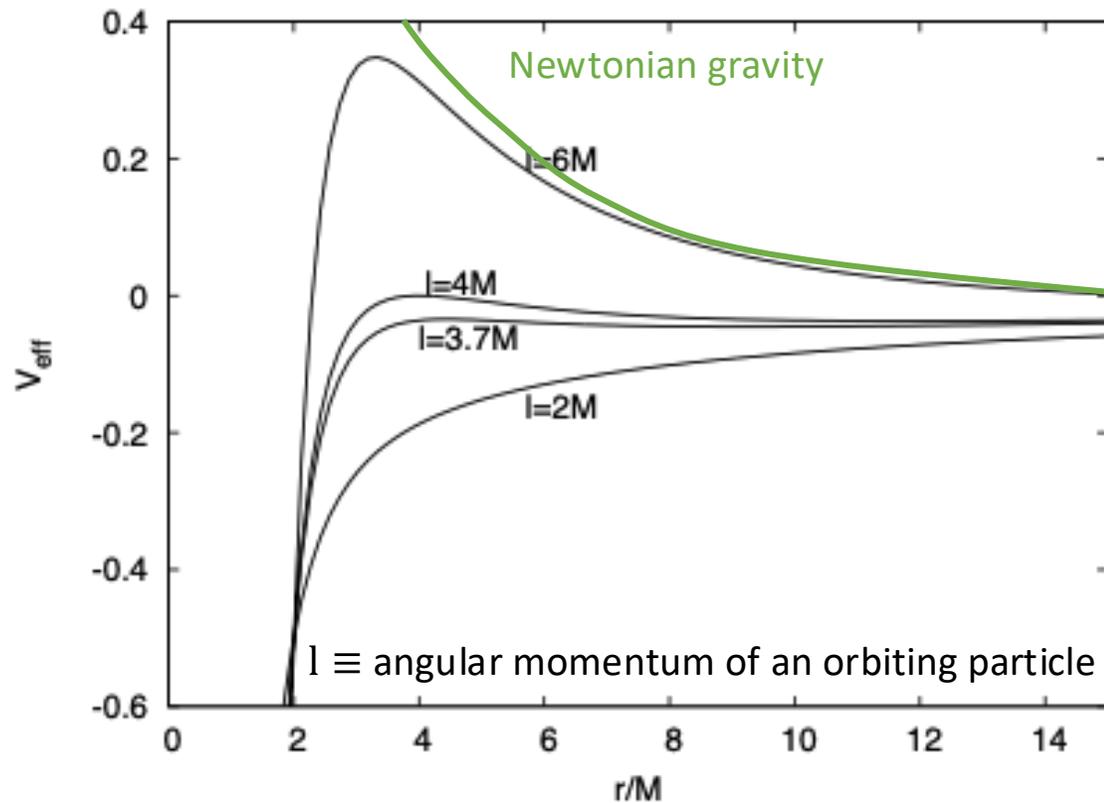


$$\begin{aligned}
 & 389 \sqrt{\frac{1}{2}} \left[2421136 \left(\frac{\sqrt{\frac{1}{2}} y \cos\left(\frac{389}{200000} \sqrt{\frac{1}{2}} (t - \sqrt{x^2 + y^2 + z^2})\right)}{\sqrt{x^2 + y^2 + z^2}} - \frac{\sqrt{\frac{1}{2}} x \sin\left(\frac{389}{200000} \sqrt{\frac{1}{2}} (t - \sqrt{x^2 + y^2 + z^2})\right)}{\sqrt{x^2 + y^2 + z^2}} \right)^2 - 453963 \left(\frac{x \cos\left(\frac{389}{200000} \sqrt{\frac{1}{2}} (t - \sqrt{x^2 + y^2 + z^2})\right)}{\sqrt{x^2 + y^2 + z^2}} + \frac{y \sin\left(\frac{389}{200000} \sqrt{\frac{1}{2}} (t - \sqrt{x^2 + y^2 + z^2})\right)}{\sqrt{x^2 + y^2 + z^2}} \right)^2 \right. \\
 & + \frac{6224000 \sqrt{\frac{1}{2}} y \cos\left(\frac{389}{200000} \sqrt{\frac{1}{2}} (t - \sqrt{x^2 + y^2 + z^2})\right)}{\sqrt{x^2 + y^2 + z^2}} - \frac{6224000 \sqrt{\frac{1}{2}} x \sin\left(\frac{389}{200000} \sqrt{\frac{1}{2}} (t - \sqrt{x^2 + y^2 + z^2})\right)}{\sqrt{x^2 + y^2 + z^2}} \\
 & + \frac{933600000 \left(\frac{\sqrt{\frac{1}{2}} y \cos\left(\frac{389}{200000} \sqrt{\frac{1}{2}} (t - \sqrt{x^2 + y^2 + z^2})\right)}{\sqrt{x^2 + y^2 + z^2}} - \frac{\sqrt{\frac{1}{2}} x \sin\left(\frac{389}{200000} \sqrt{\frac{1}{2}} (t - \sqrt{x^2 + y^2 + z^2})\right)}{\sqrt{x^2 + y^2 + z^2}} \right) \left(\frac{x \cos\left(\frac{389}{200000} \sqrt{\frac{1}{2}} (t - \sqrt{x^2 + y^2 + z^2})\right)}{\sqrt{x^2 + y^2 + z^2}} + \frac{y \sin\left(\frac{389}{200000} \sqrt{\frac{1}{2}} (t - \sqrt{x^2 + y^2 + z^2})\right)}{\sqrt{x^2 + y^2 + z^2}} \right)}{\sqrt{x^2 + y^2 + z^2}} \\
 & + \frac{240000000000 \left(\frac{x \cos\left(\frac{389}{200000} \sqrt{\frac{1}{2}} (t - \sqrt{x^2 + y^2 + z^2})\right)}{\sqrt{x^2 + y^2 + z^2}} + \frac{y \sin\left(\frac{389}{200000} \sqrt{\frac{1}{2}} (t - \sqrt{x^2 + y^2 + z^2})\right)}{\sqrt{x^2 + y^2 + z^2}} \right)^2}{x^2 + y^2 + z^2} + \frac{320000000 \left(\frac{x \cos\left(\frac{389}{200000} \sqrt{\frac{1}{2}} (t - \sqrt{x^2 + y^2 + z^2})\right)}{\sqrt{x^2 + y^2 + z^2}} + \frac{y \sin\left(\frac{389}{200000} \sqrt{\frac{1}{2}} (t - \sqrt{x^2 + y^2 + z^2})\right)}{\sqrt{x^2 + y^2 + z^2}} \right)}{\sqrt{x^2 + y^2 + z^2}} \\
 & \left. + \frac{80000000000 \left(\cos\left(\frac{389}{200000} \sqrt{\frac{1}{2}} (t - \sqrt{x^2 + y^2 + z^2})\right)^2 + \sin\left(\frac{389}{200000} \sqrt{\frac{1}{2}} (t - \sqrt{x^2 + y^2 + z^2})\right)^2 \right)}{x^2 + y^2 + z^2} \right]
 \end{aligned}$$



Example of a direct effect from GR

- Around a Schwarzschild black hole exists a so-called « innermost stable circular orbit » (ISCO) – Fig. 4.1 of your lecture notes



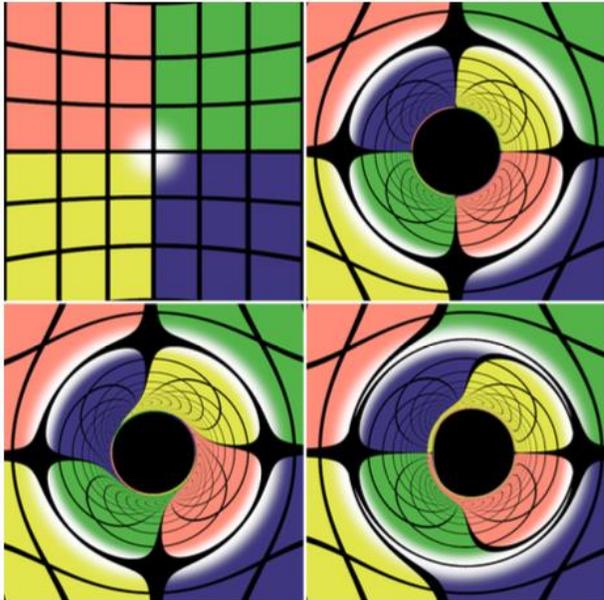
$l \nearrow \Rightarrow$ centrifugal force (outward) \nearrow

- An accretion disk should be truncated at this ISCO

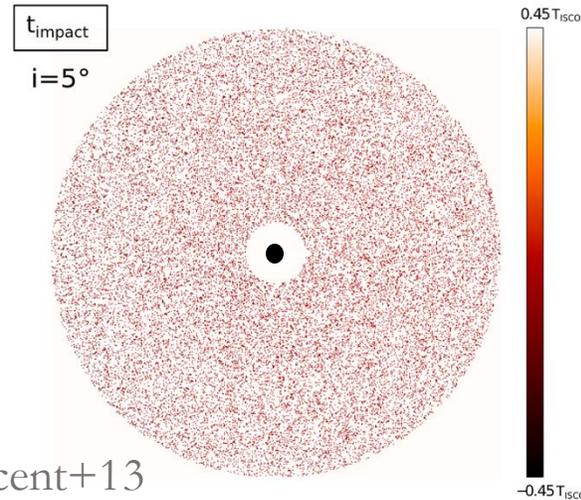


Why using a GR ray-tracing code ?

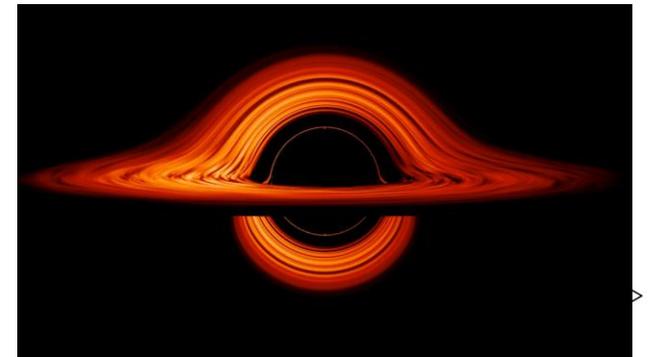
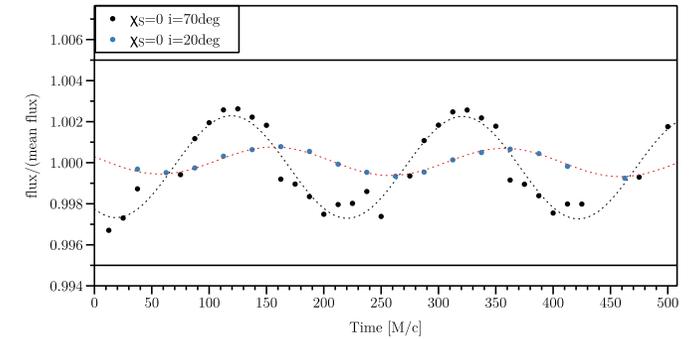
- **Concept:** solve the geodesic equation for photons back from the observer (Earth) to the source
- **Relativistic ray-tracing:**
 - e.g. Doppler beaming: matter approaching the observer appears brighter
→ an orbiting dense blob produces a sinusoid in the luminosity
- **GR effects:**
 - Light deflection (p. 57)
 - « Shapiro effect »: time delay



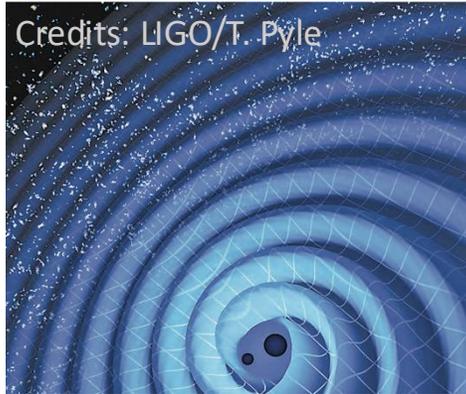
Bohn+15



Vincent+13



Inspiral equation of motion



zero \Leftrightarrow circular orbit

$$\dot{E} = -\mathcal{F} - \dot{M}$$

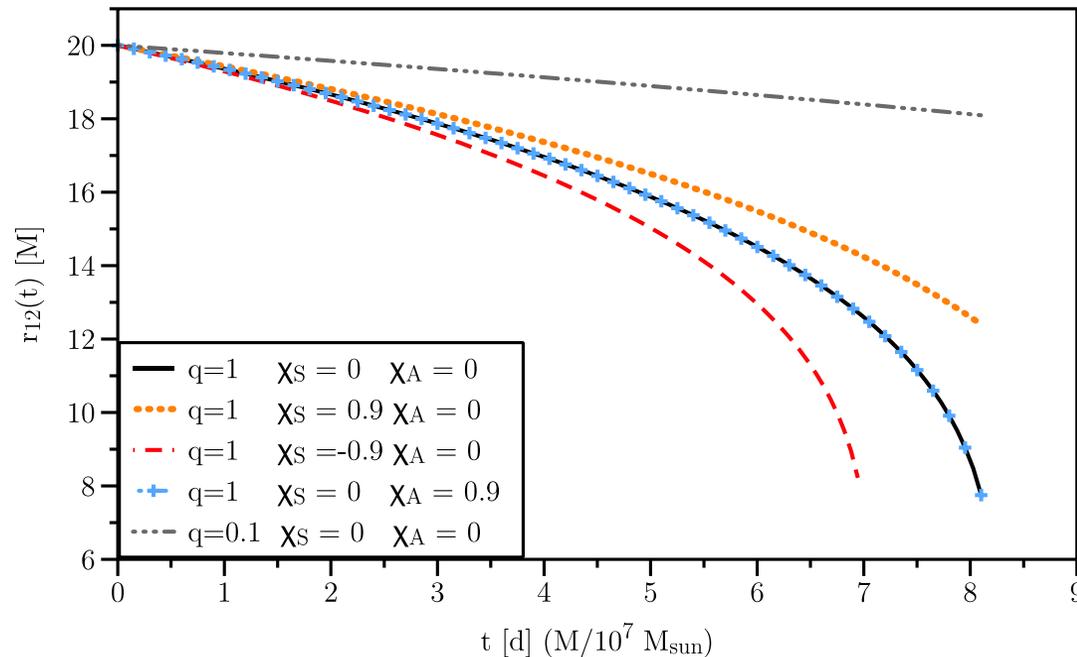
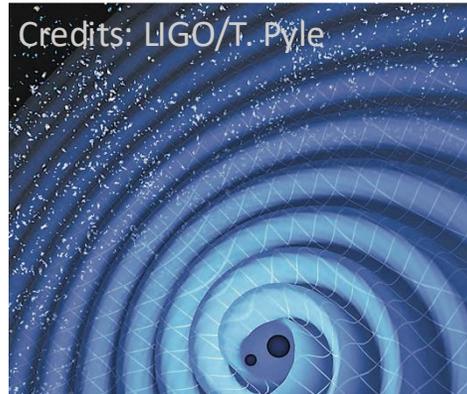
Rate of change of orbital binding energy

\rightarrow

$$\frac{dt}{dr_{12}} = -\frac{dE(r_{12})/dr_{12}}{\mathcal{F}(r_{12}) + \dot{M}(r_{12})}$$

Change in mass
(« tidal heating »)

Inspirational equation of motion



zero \Leftrightarrow circular orbit

$$\dot{E} = -\mathcal{F} - \dot{M}$$

Rate of change of orbital binding energy

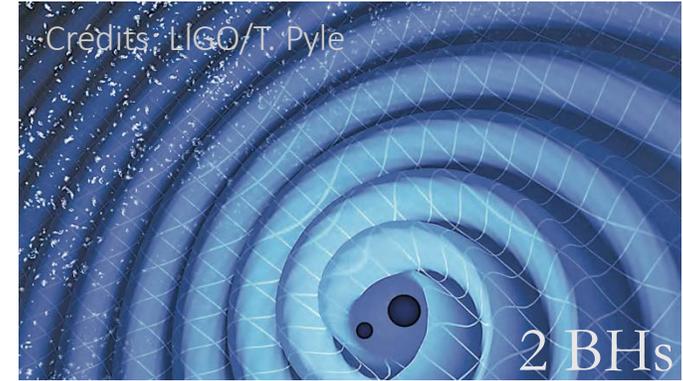
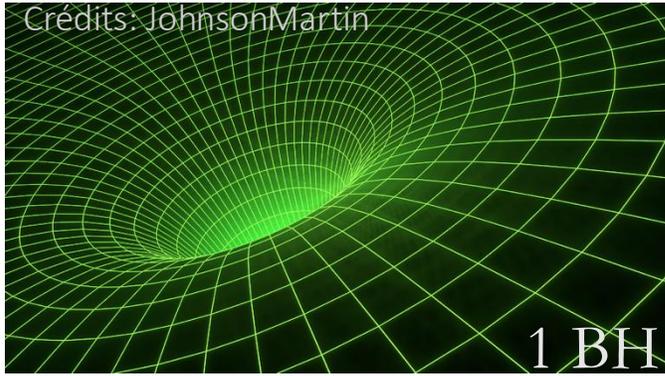


$$\frac{dt}{dr_{12}} = - \frac{dE(r_{12})/dr_{12}}{\mathcal{F}(r_{12}) + \dot{M}(r_{12})}$$

Change in mass
(« tidal heating »)

- 3.5 Post-Newtonian equation of motion validated
- Slower inspiral for $q \searrow$

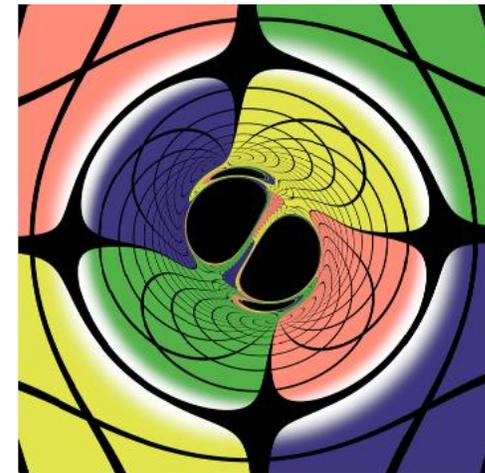
From single to binary black holes



$$g_{\mu\nu} = \begin{pmatrix} 1 + \frac{2Mr}{\rho^2} & 0 & 0 & \frac{4Mar\sin^2\theta}{\rho^2} \\ 0 & -\rho^2/\Delta & 0 & 0 \\ 0 & 0 & -\rho^2 & 0 \\ \frac{4Mar\sin^2\theta}{\rho^2} & 0 & 0 & -(r^2 + a^2 + \frac{2Ma^2r\sin^2\theta}{\rho^2})\sin^2\theta \end{pmatrix}$$

~~Stationarity~~
 Delayed gravity
~~Axisymmetry~~

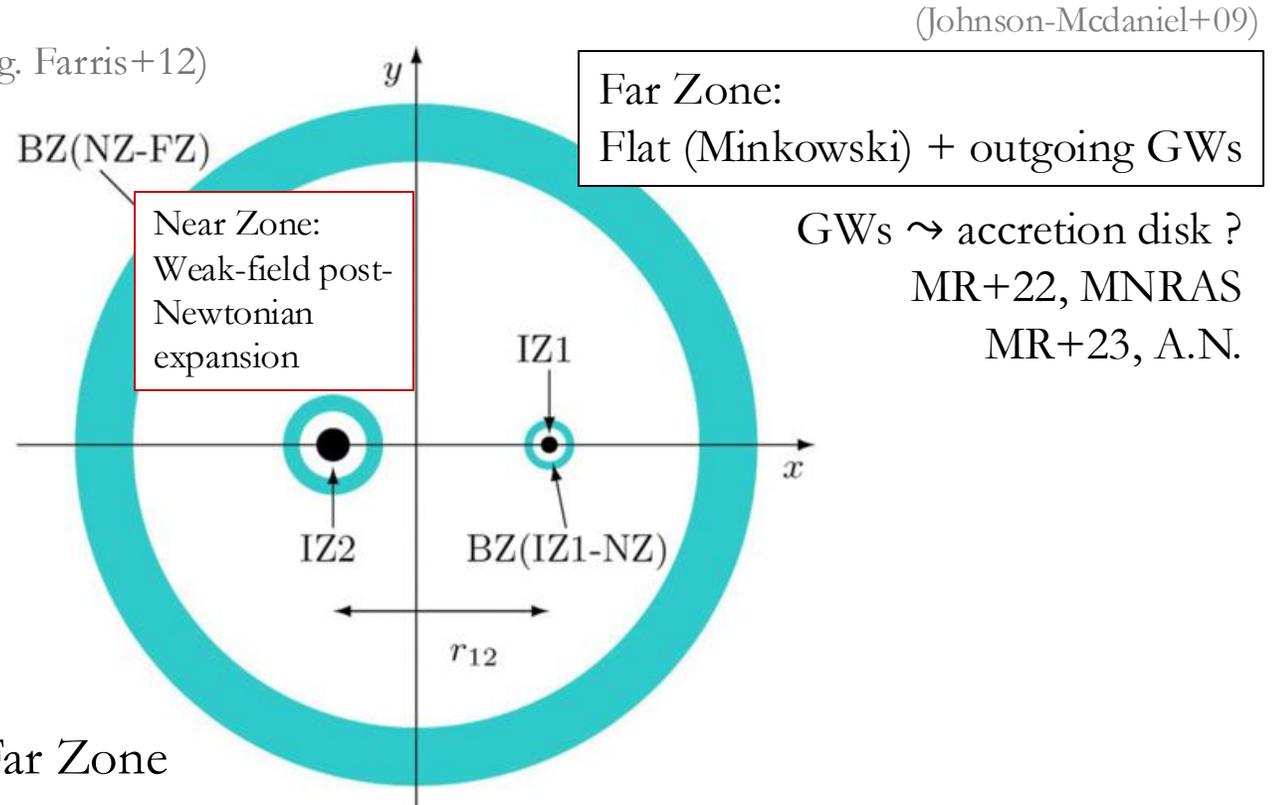
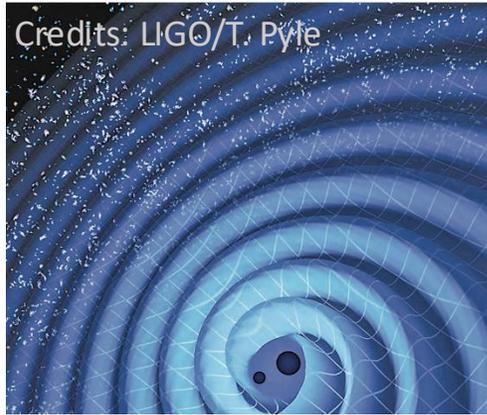
$$g_{\mu\nu} = \begin{pmatrix} g_{tt} & g_{tr} & g_{t\theta} & g_{t\phi} \\ g_{rt} & g_{rr} & g_{r\theta} & g_{r\phi} \\ g_{\theta t} & g_{\theta r} & g_{\theta\theta} & g_{\theta\phi} \\ g_{\phi t} & g_{\phi r} & g_{\phi\theta} & g_{\phi\phi} \end{pmatrix}$$



Bohn+15

An approximate binary black hole spacetime

- Why not using Newtonian gravity ? (e.g. D’Orazio+13)
GR IS important !!
- Why not solving the Einstein’s equations ?
Too expensive for >10 orbits simulations (e.g. Farris+12)

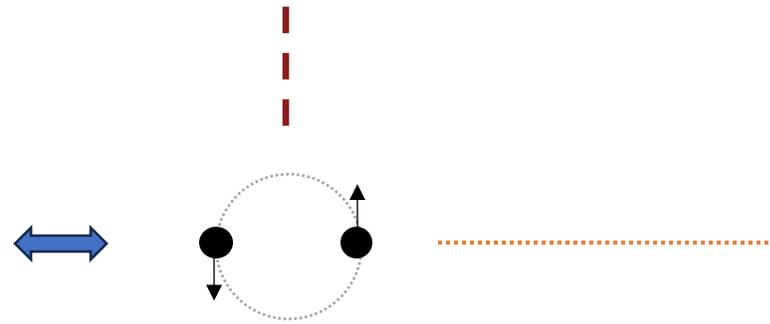
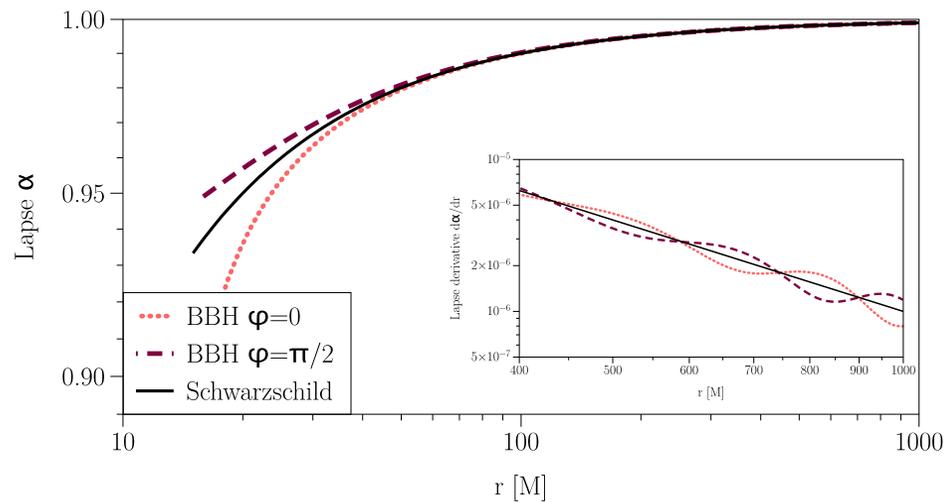


- A computationally-heavy construction: example Far Zone

$$g_{00} + 1 = \frac{2m_1}{r} + \frac{m_1}{r} \left\{ v_1^2 - \frac{m_2}{b} + 2(\vec{v}_1 \cdot \hat{n})^2 - \frac{2m}{r} + 6 \frac{(\vec{x}_1 \cdot \hat{n})}{r} (\vec{v}_1 \cdot \hat{n}) - \frac{x_1^2}{r^2} + \frac{(\vec{x}_1 \cdot \hat{n})^2}{r^2} (3 - 2r^2 \omega^2) \right\} + (1 \leftrightarrow 2) + O(v^5),$$

- Construction valid down to $r_{12} \sim 8M$ (because $v > 0.1 c$, slow-motion approx. for PN breaks down)

What does a binary black hole metric look like?



➤ Far from the binary, similar to a single BH, except for GW residual

$g_{t\phi} \neq 0 \rightarrow ?$

$$g_{\mu\nu} = \begin{pmatrix} 1 + \frac{2Mr}{\rho^2} & 0 & 0 & \frac{4Ma\sin^2\theta}{\rho^2} \\ 0 & -\rho^2/\Delta & 0 & 0 \\ 0 & 0 & -\rho^2 & 0 \\ \frac{4Ma\sin^2\theta}{\rho^2} & 0 & 0 & -(r^2 + a^2 + \frac{2Ma^2r\sin^2\theta}{\rho^2})\sin^2\theta \end{pmatrix}$$

➤ Frame-dragging (Lense-Thirring) effect, as in the Kerr metric, but due to the orbital motion of the BBH

